



EECS 230 Deep Learning

Lecture 8: Image Segmentation

Part I

Some slides from Yuri Boykov

From last lecture: Convolutional Layer

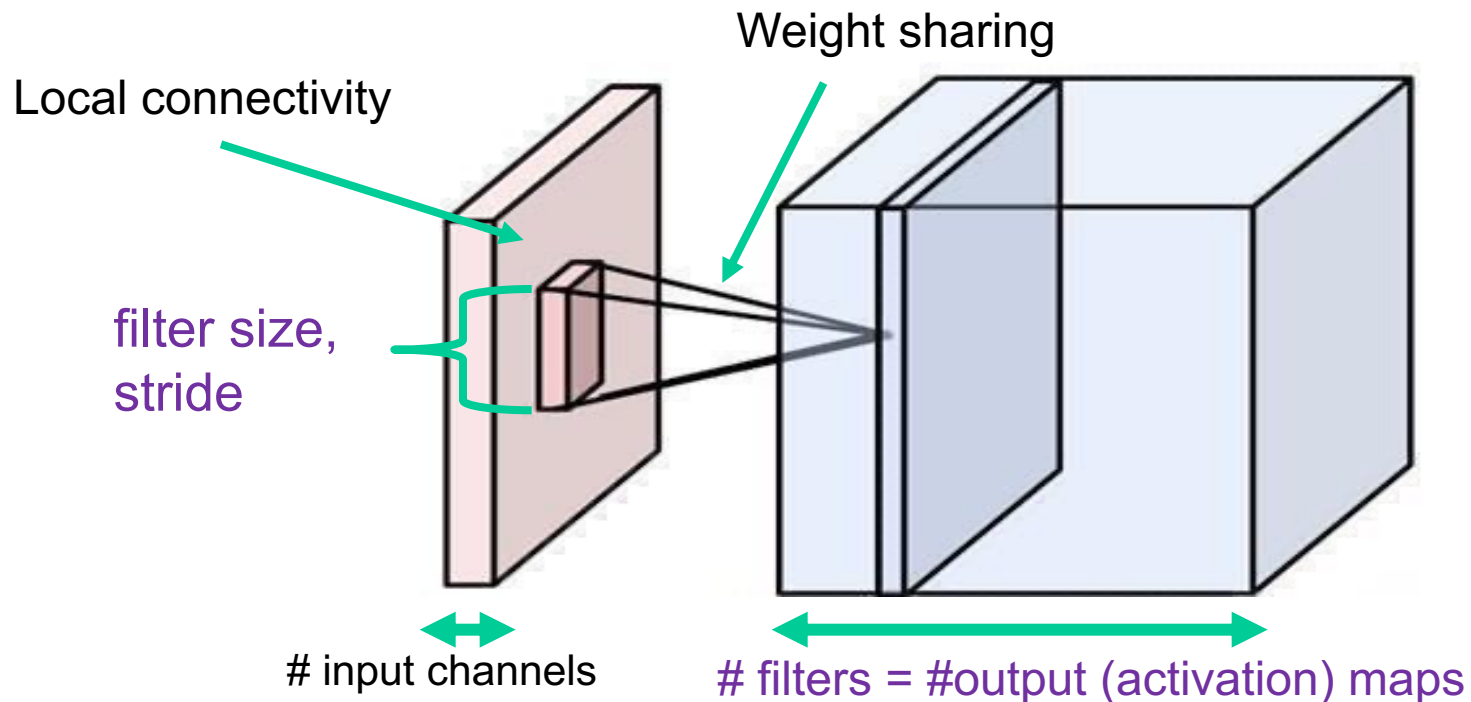
Local connectivity

Weight sharing

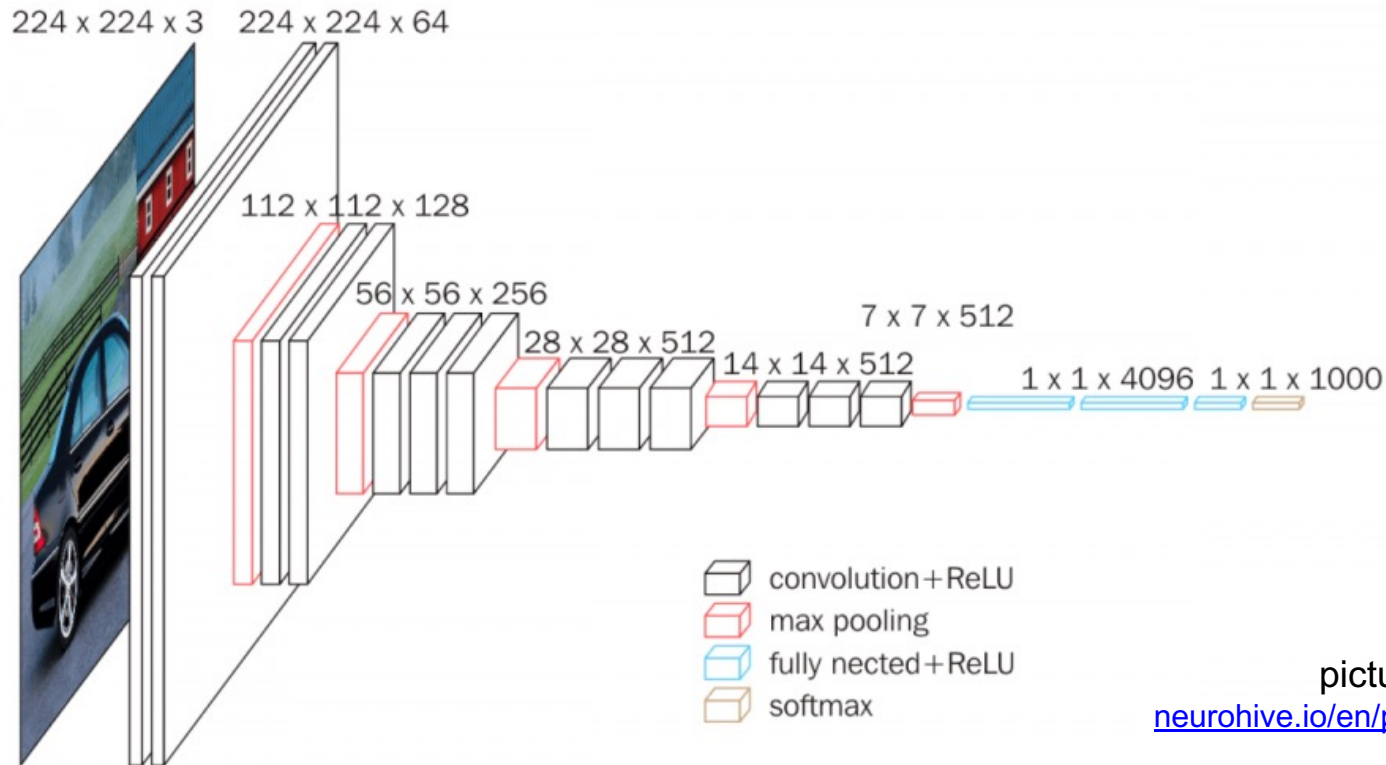
Handling multiple input/output channels

Retains location associations

Transforms 3D tensor into 3D tensor

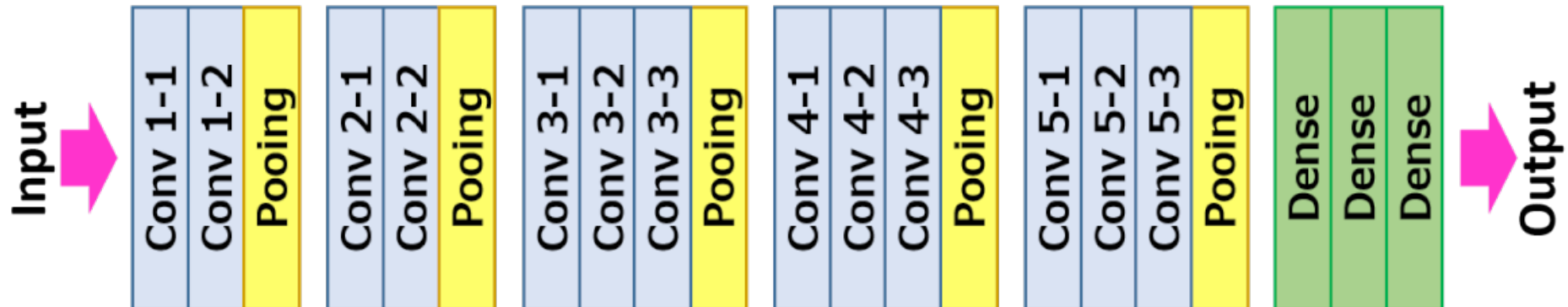


From last lecture: CNN e.g. VGG -16



picture credits

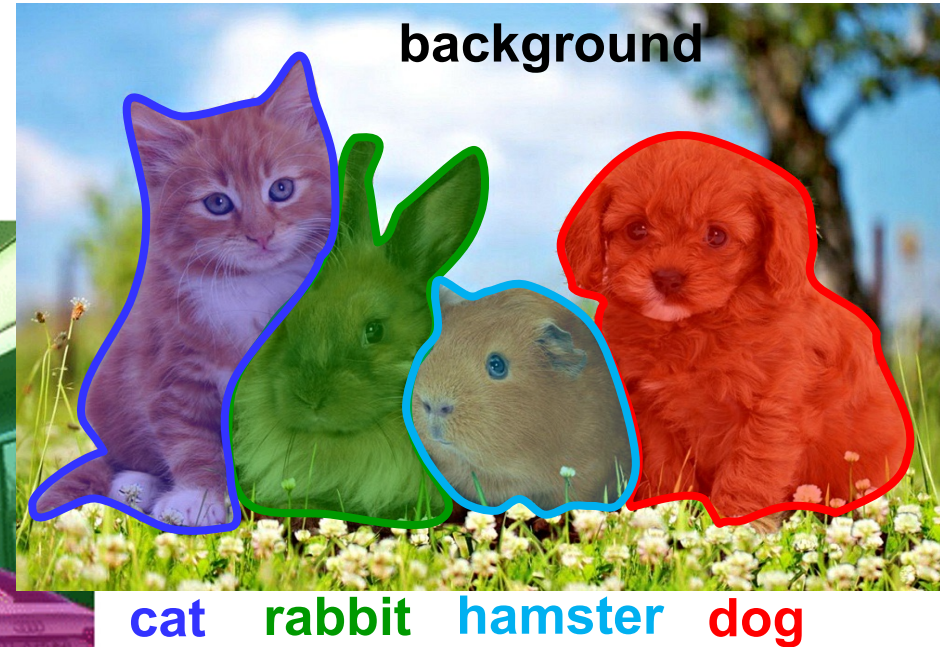
neurohive.io/en/popular-networks/vgg16/





CNN for Image Segmentation

Semantic Segmentation



Semantic Segmentation (outline)

- ❑ From image labeling to **pixel labeling**
- ❑ Architectures
- ❑ Training loss function
- ❑ Evaluation metrics
- ❑ Weakly supervised segmentation

input



learn to

predict

remember last topic: image classification

somewhere in the image
there is a **bicycle** and a **person**

image **tags**
(image-level labels)

Semantic Segmentation

input



learn to
predict



pixel-level labels

person

bicycle

background

Fully-supervised Semantic Segmentation

training uses pixel-accurate Ground Truth

input



target (GT mask)



learn to
predict



pixel-level labels

person

bicycle

background

Fully-supervised Semantic Segmentation

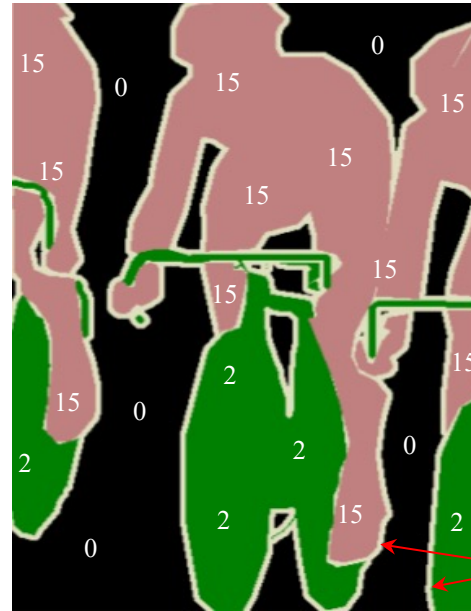
training uses pixel-accurate Ground Truth

input



target (GT mask)

learn to
predict



pixel-level labels

person

bicycle

background

255 (void/undefined)

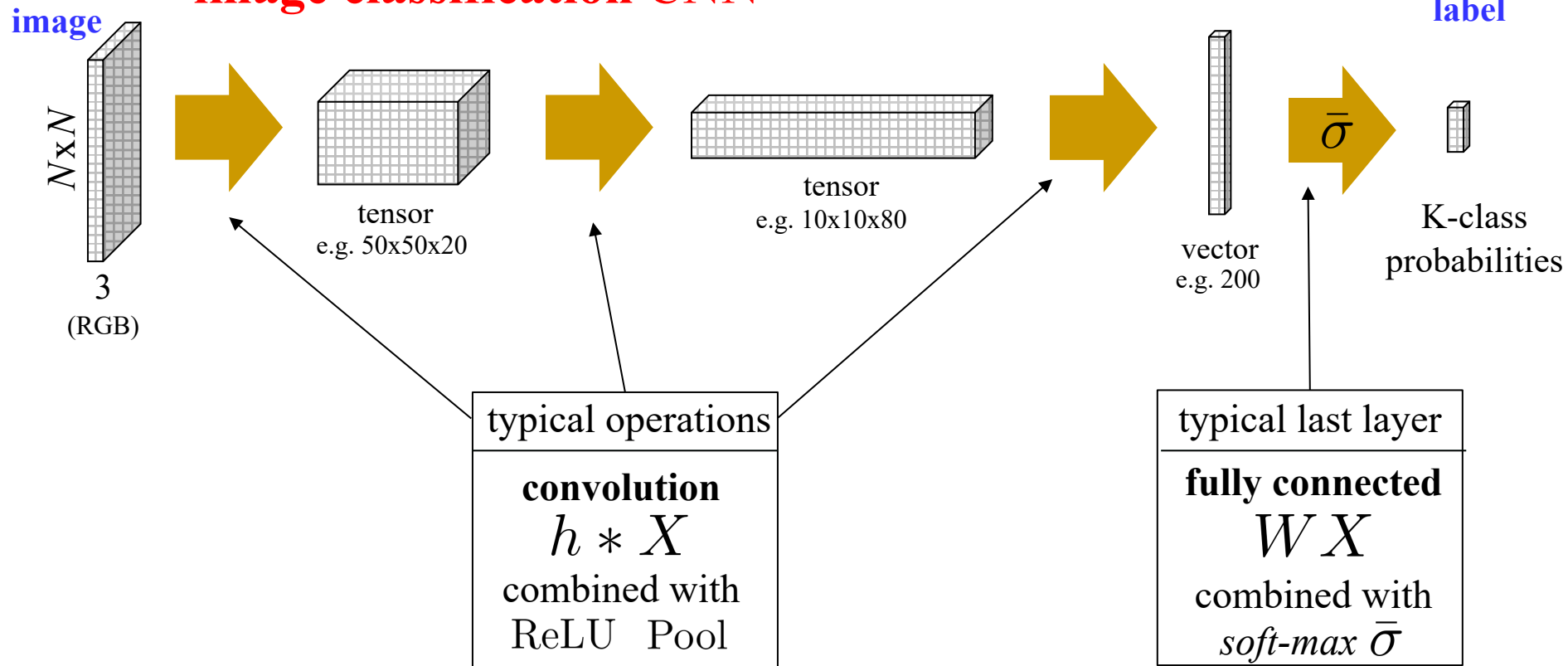
$y^p \in [0, 1, 2, 3, \dots]$ - class label at each pixel p

pixel labels (object classes) used in Pascal dataset:

- 0 - *background*
- 1-20 - airplane, bicycle, bird, boat, bottle, bus, car, cat, chair, cow, dining table, dog, horse, motorbike, person, potted plant, sheep, sofa, train, TV monitor
- 255 - *void* (class for pixel is undefined)

From Image to Pixel Labeling

image classification CNN

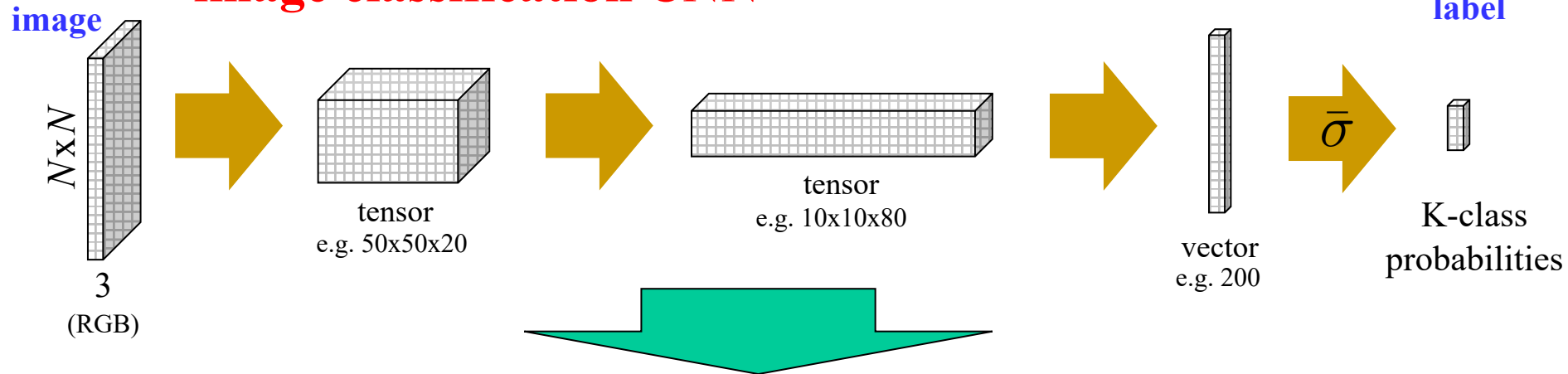


Q: How do we go from here to image segmentation?

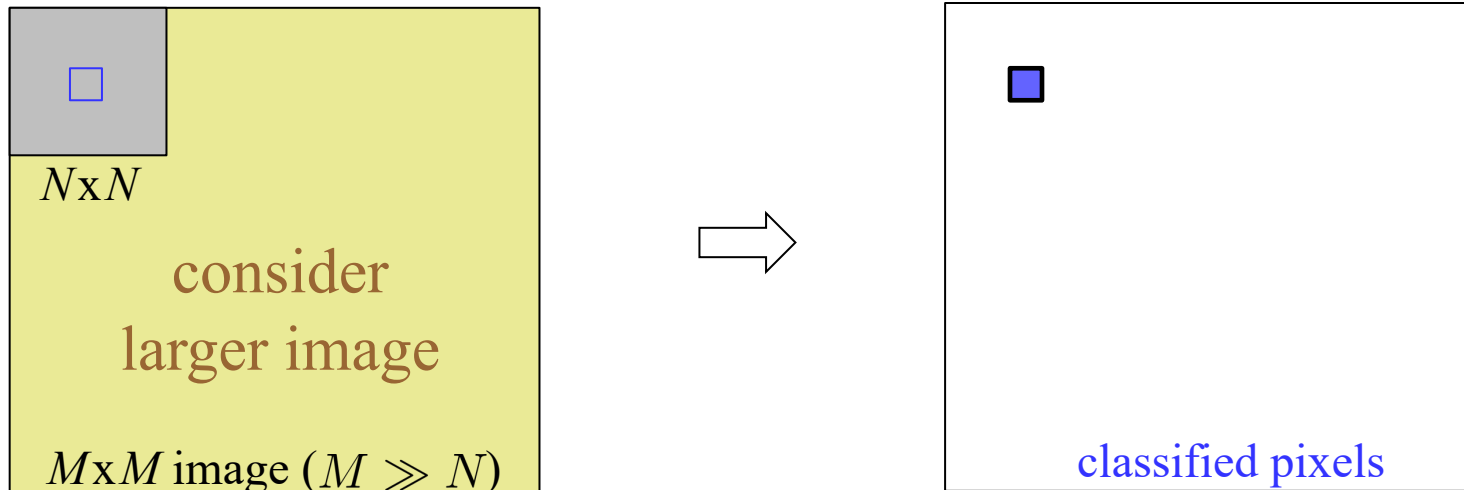
That is, how to extend NN methods for image classification to **classification of image pixels** ?

From Image to Pixel Labeling

image classification CNN

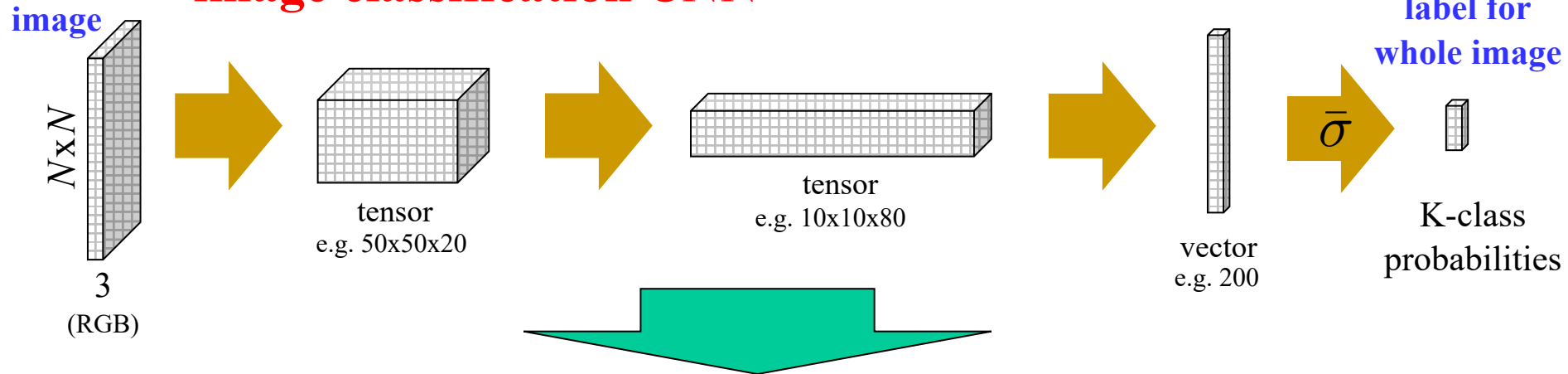


First (naïve) idea: classify pixels using *sliding windows*

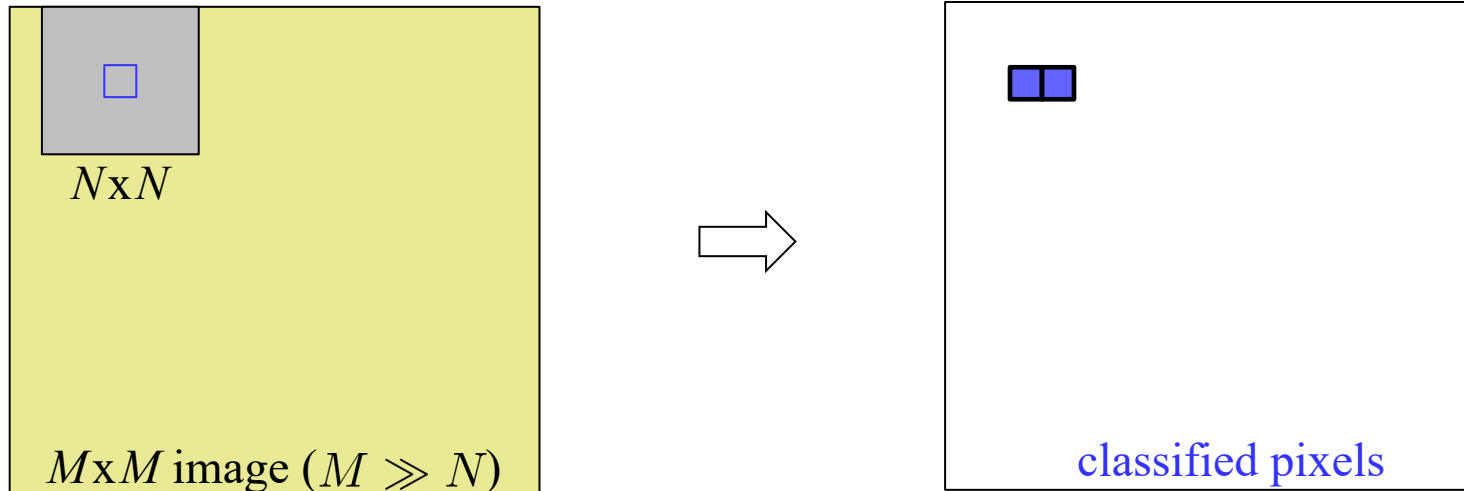


From Image to Pixel Labeling

image classification CNN

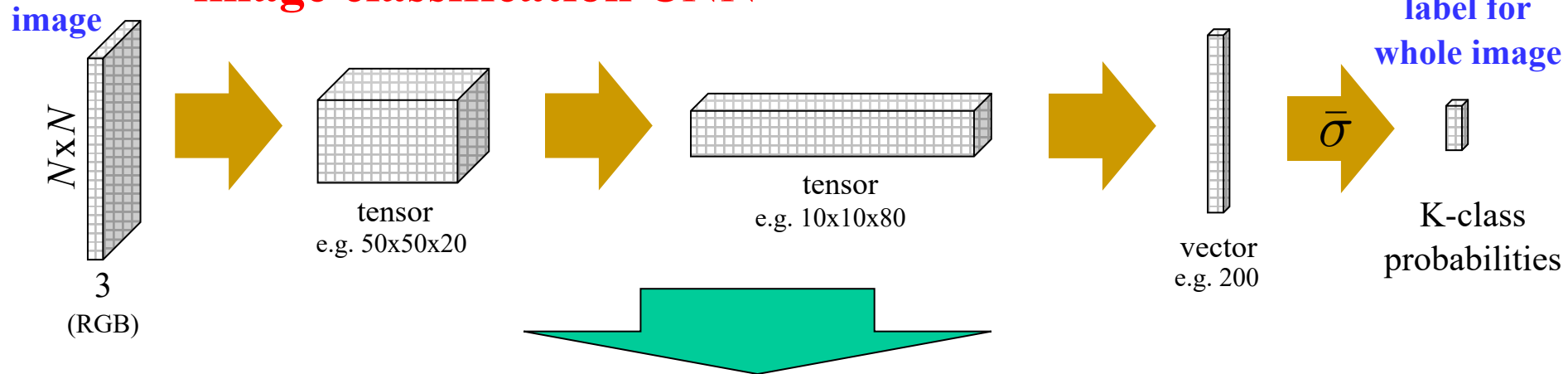


First (naïve) idea: classify pixels using *sliding windows*

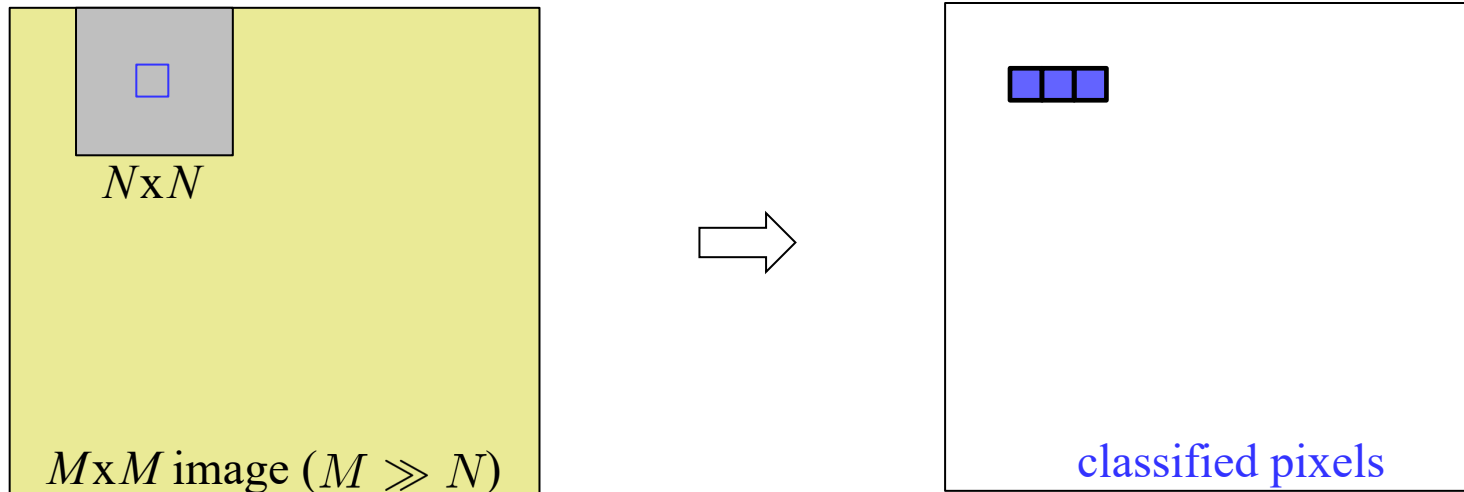


From Image to Pixel Labeling

image classification CNN

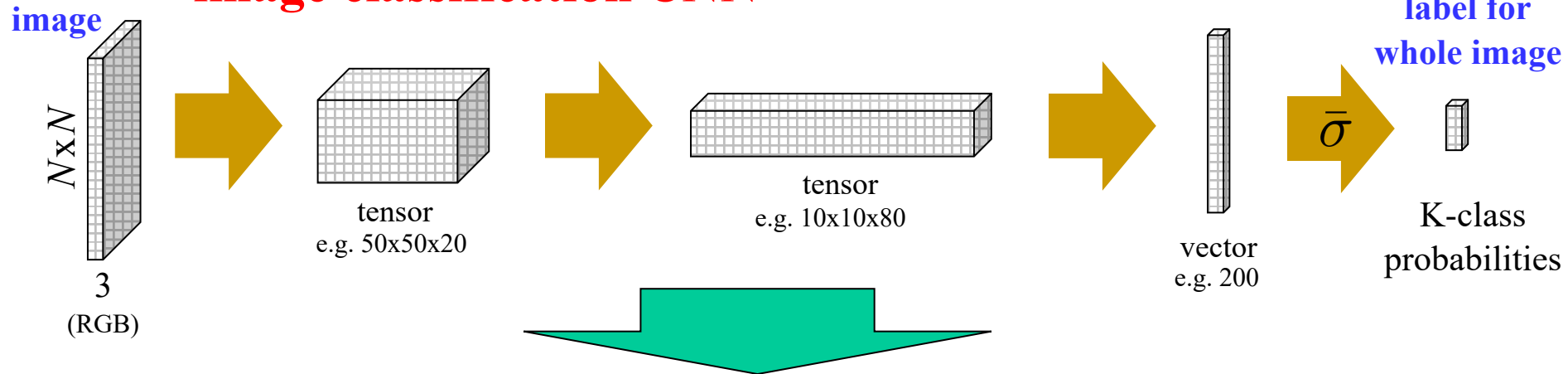


First (naïve) idea: classify pixels using *sliding windows*

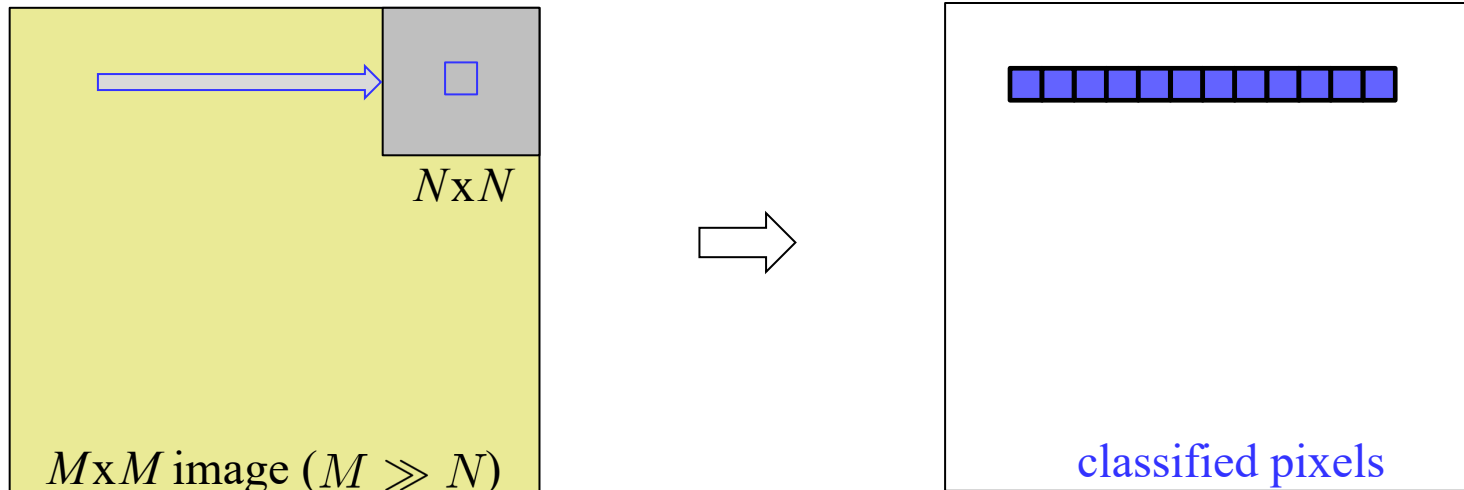


From Image to Pixel Labeling

image classification CNN

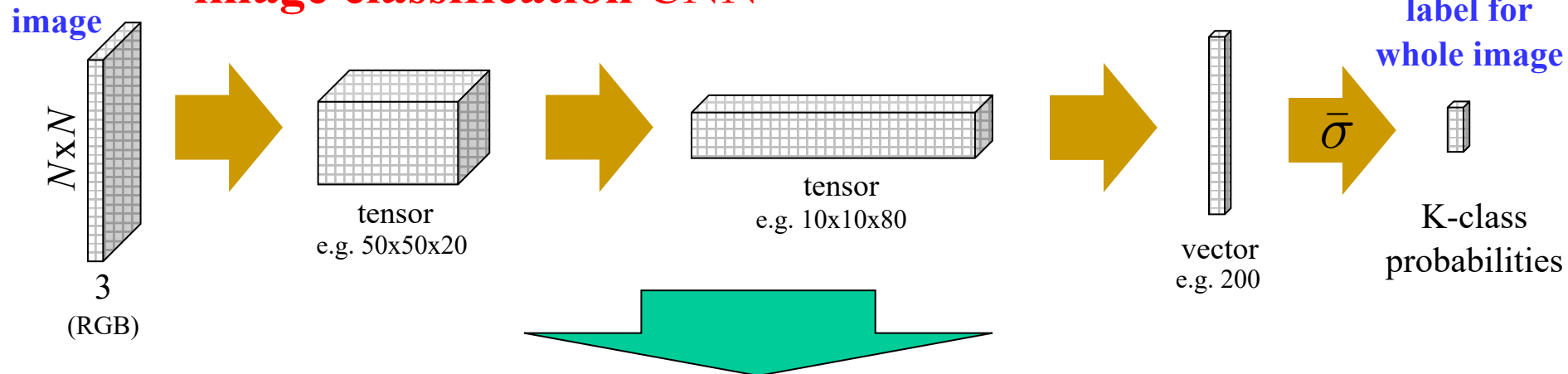


First (naïve) idea: classify pixels using *sliding windows*

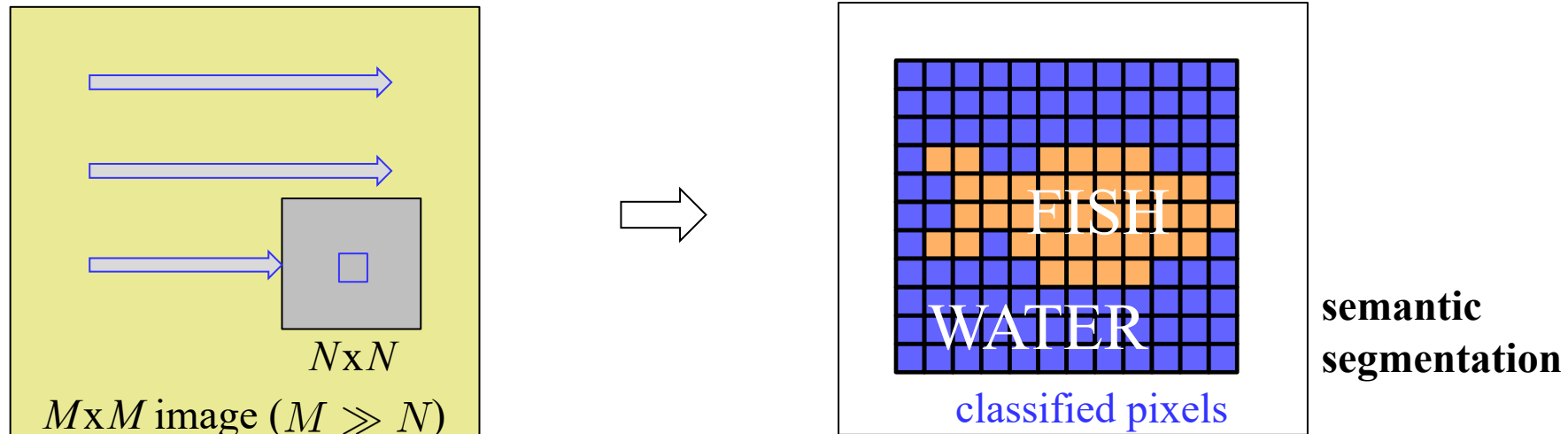


From Image to Pixel Labeling

image classification CNN



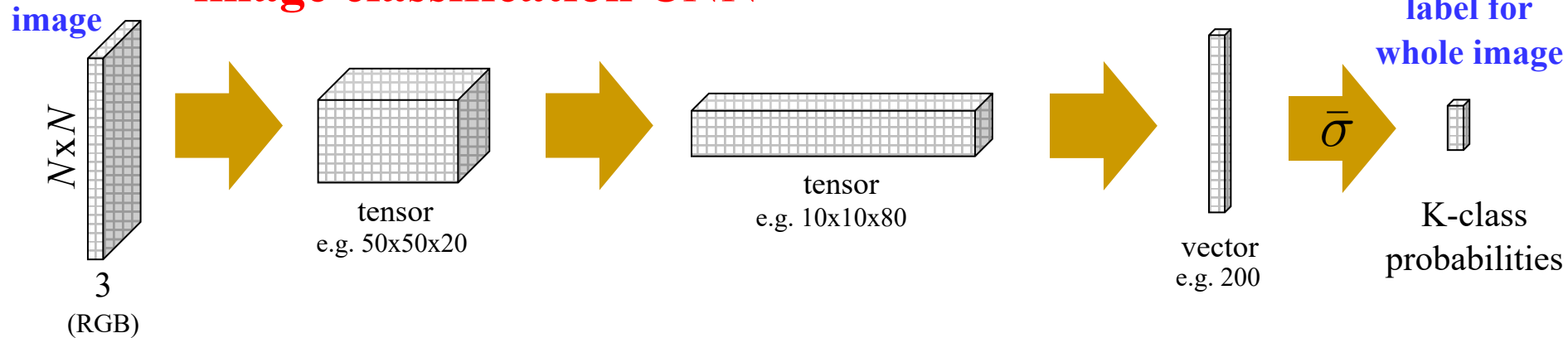
First (naïve) idea: classify pixels using *sliding windows*



Not bad for a start, but pixels are classified independently (one-at-a-time). For example, such **one-pixel classifying network** can NOT learn **spatial pattern** of the **whole** GT segmentation mask.

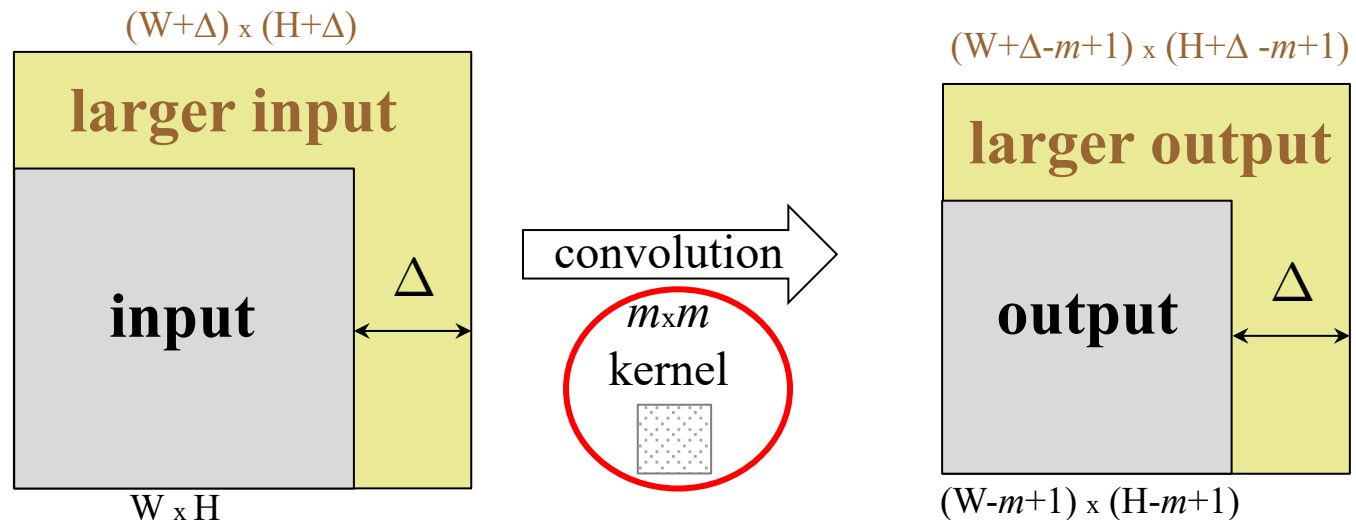
From Image to Pixel Labeling

image classification CNN



Better idea: convolutional kernel can be applied to input of any size!

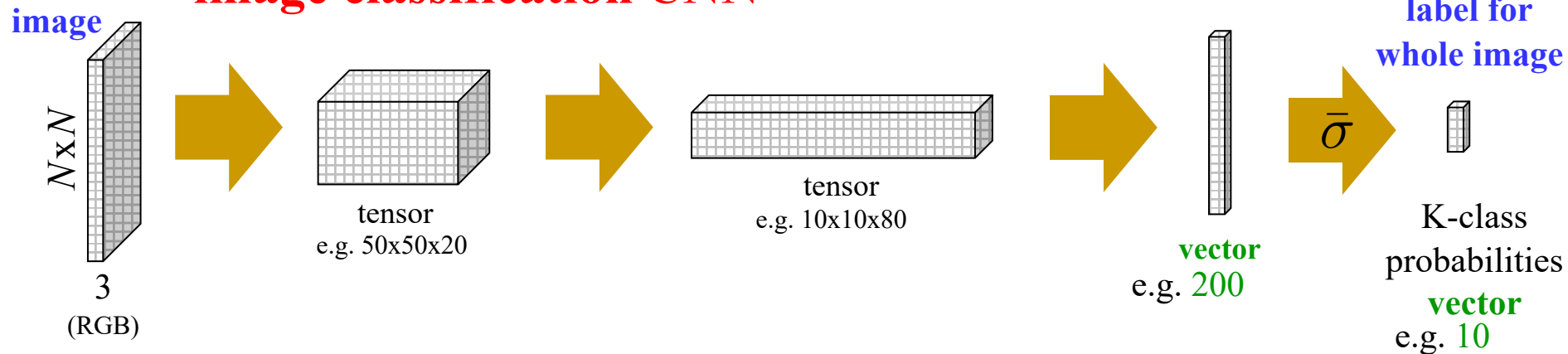
Key insight:



using the same kernel

From Image to Pixel Labeling

image classification CNN



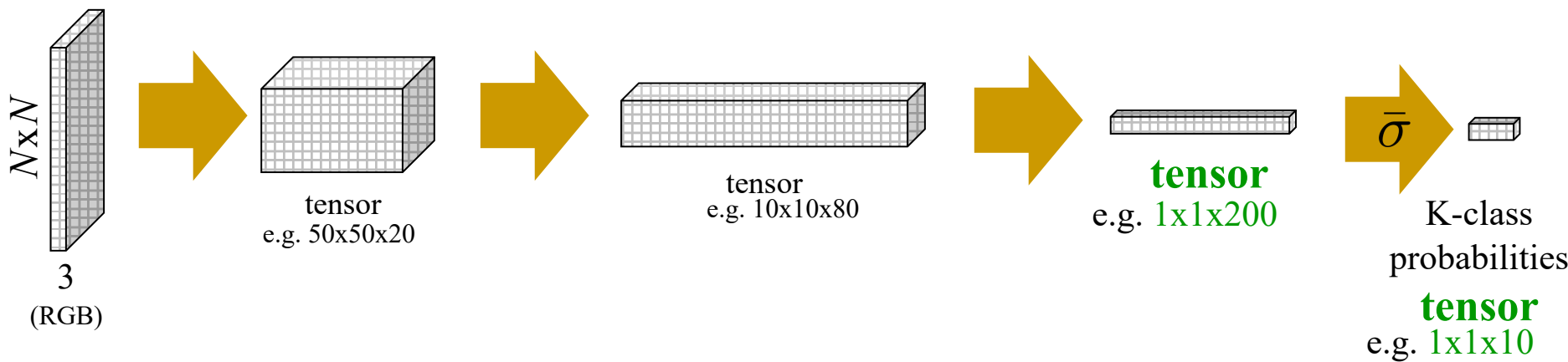
Better idea: convolutional kernel can be applied to input of any size!

Assume **all layers are convolutional**.

What about last (fully connected) layer?

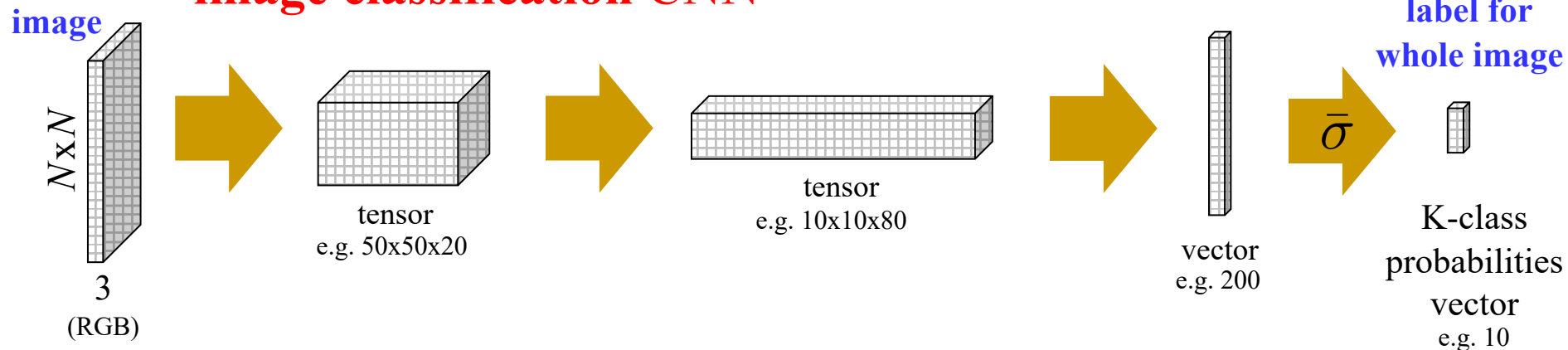
No problem:

$$W_{10 \times 200} X \equiv h_{1 \times 1}^{200 \rightarrow 10} * X$$



From Image to Pixel Labeling

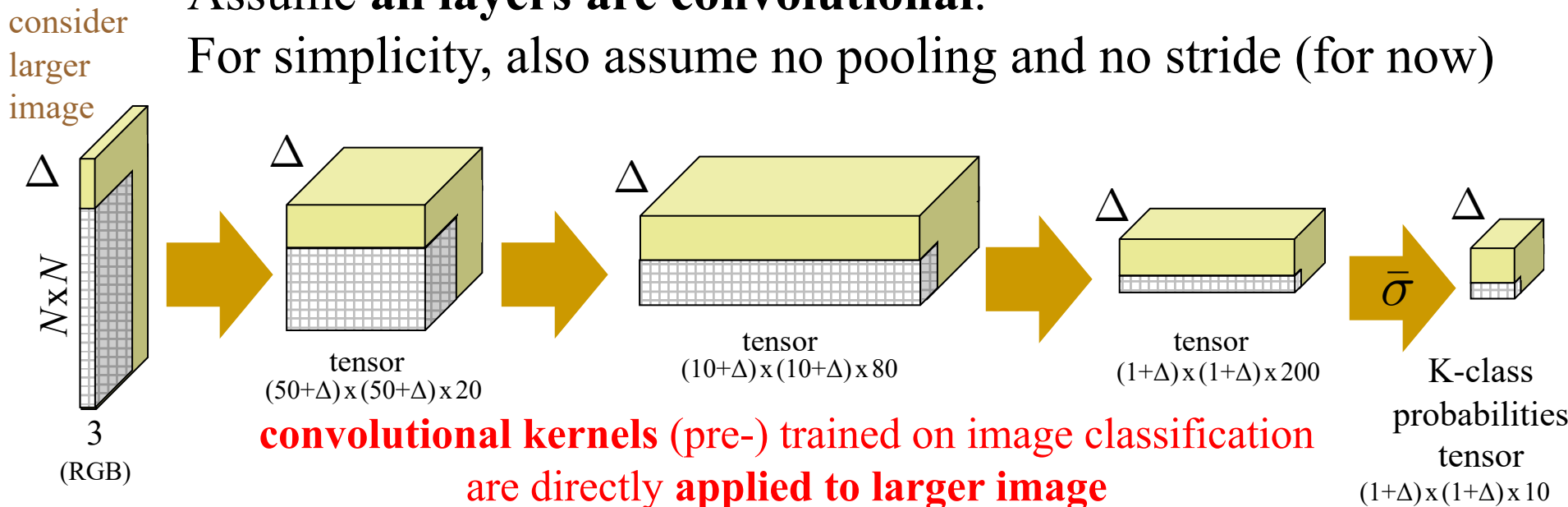
image classification CNN



Better idea: convolutional kernel can be applied to input of any size!

Assume **all layers are convolutional**.

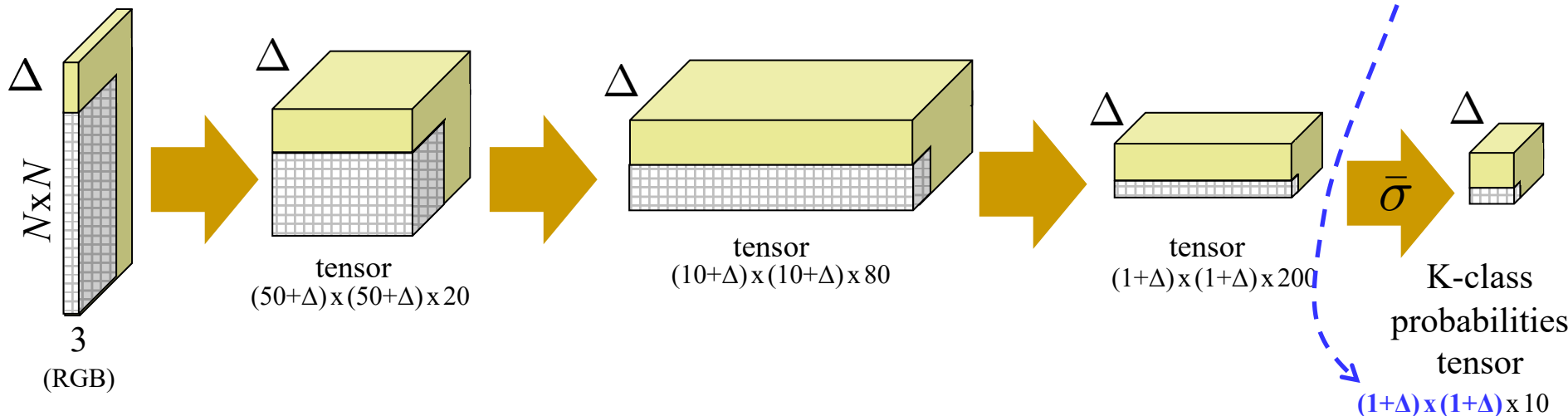
For simplicity, also assume no pooling and no stride (for now)



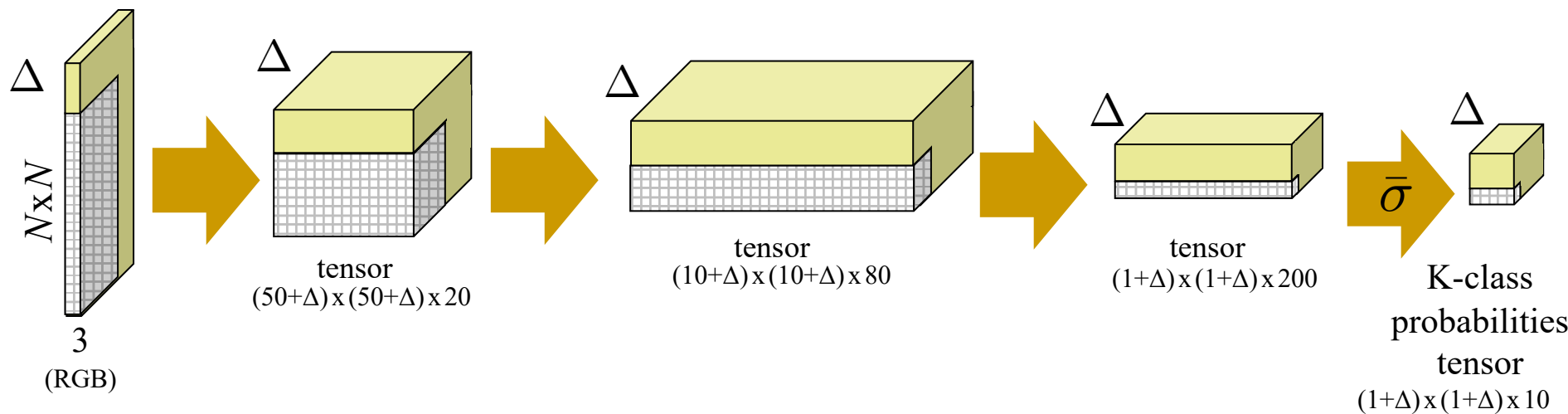
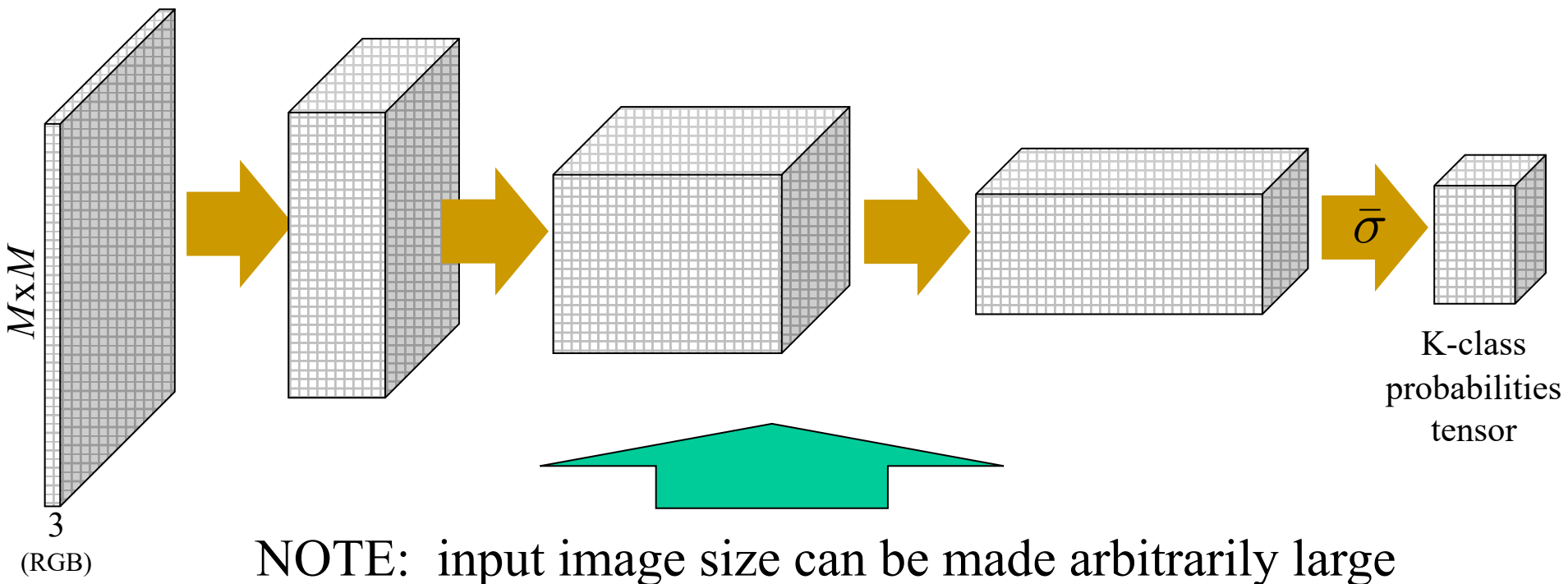
From Image to Pixel Labeling

Now, network output has some spatial resolution!

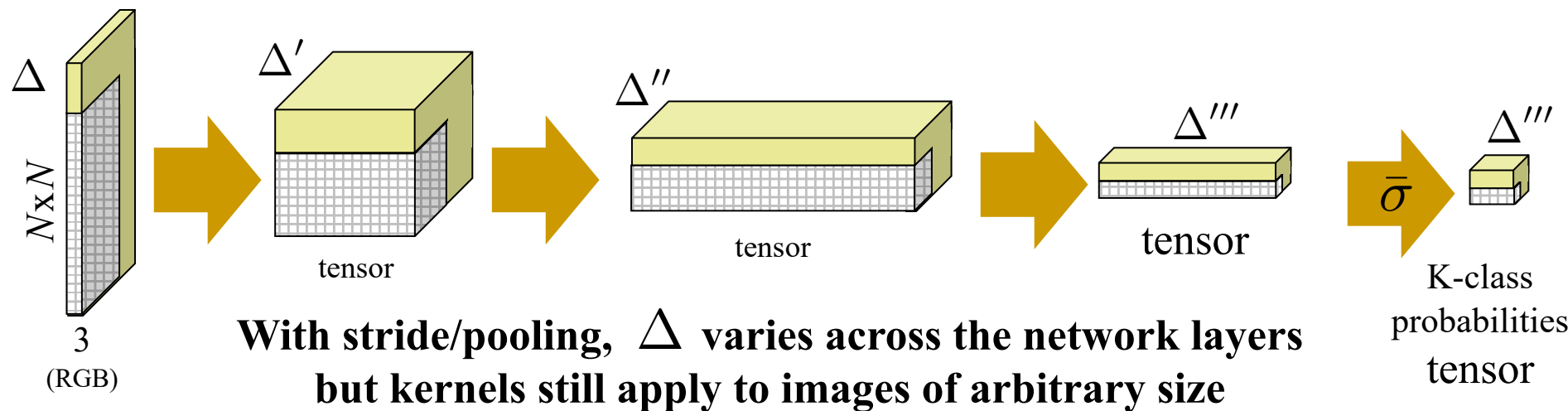
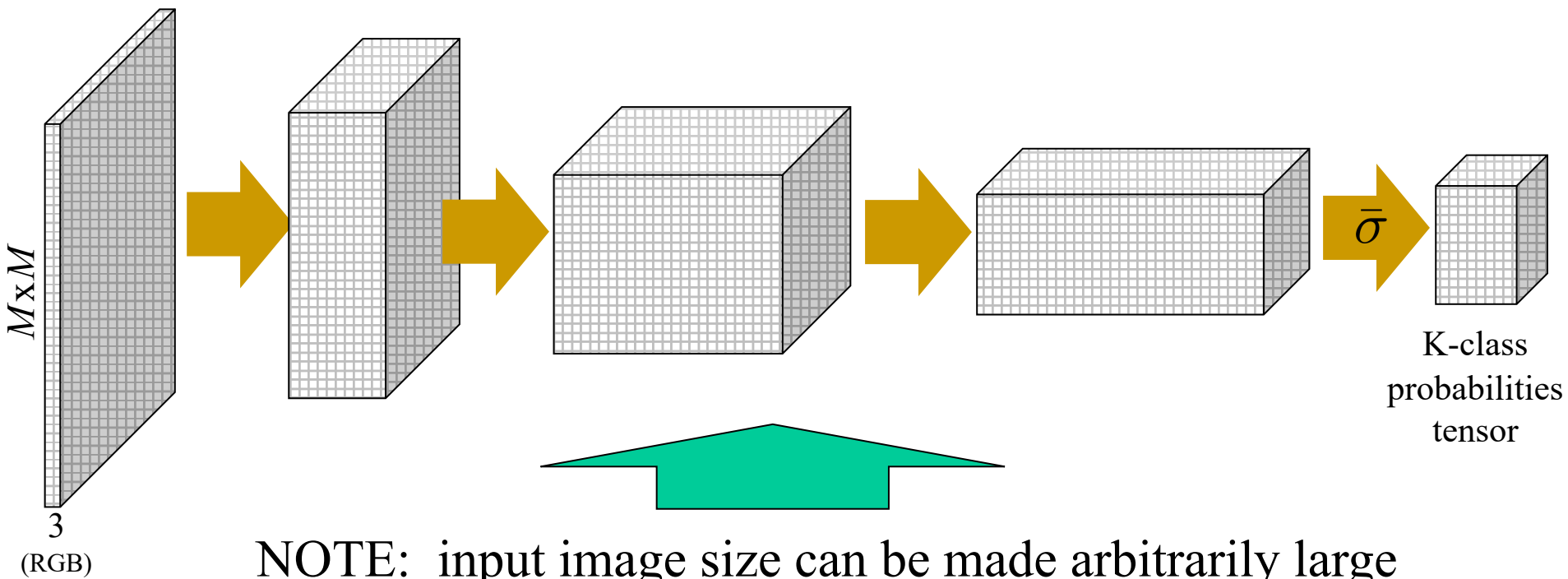
Intuition: K-class probabilities in the gray part of the output have “*receptive field*” in the gray part of the input image, while yellow output is supported by different $N \times N$ sections of the larger image



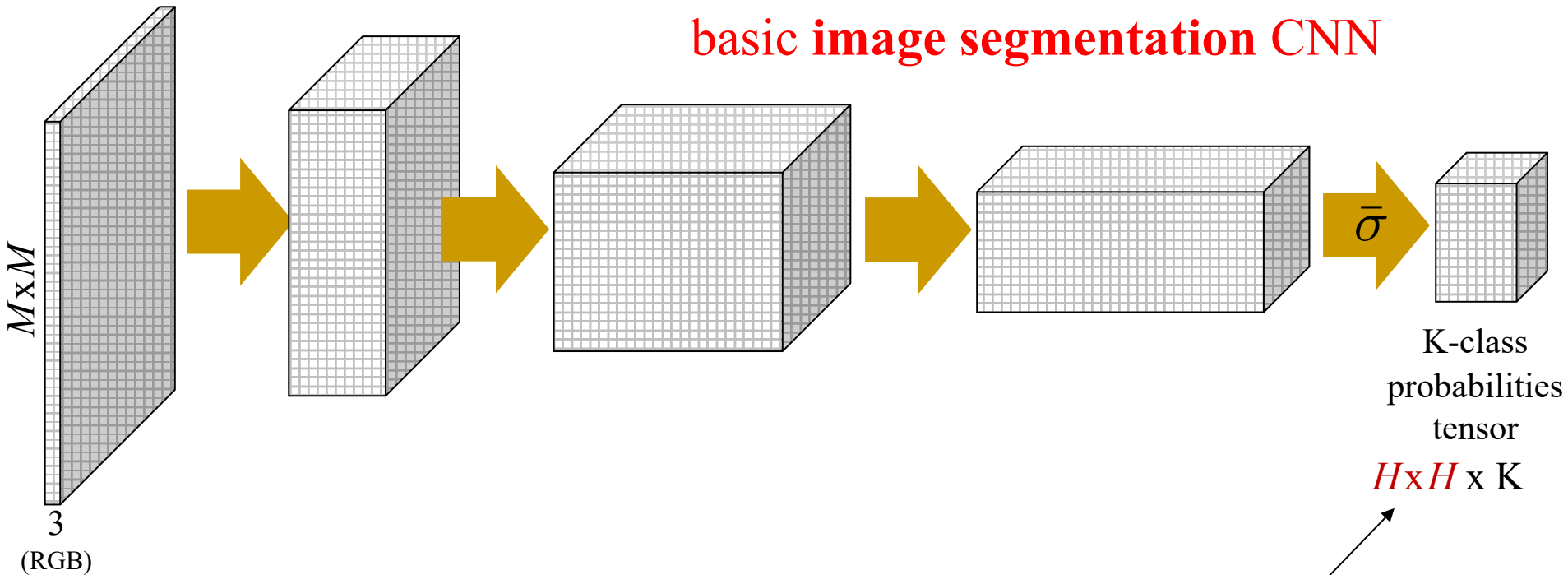
Fully Convolutional Network (FCN)



Fully Convolutional Network (FCN)



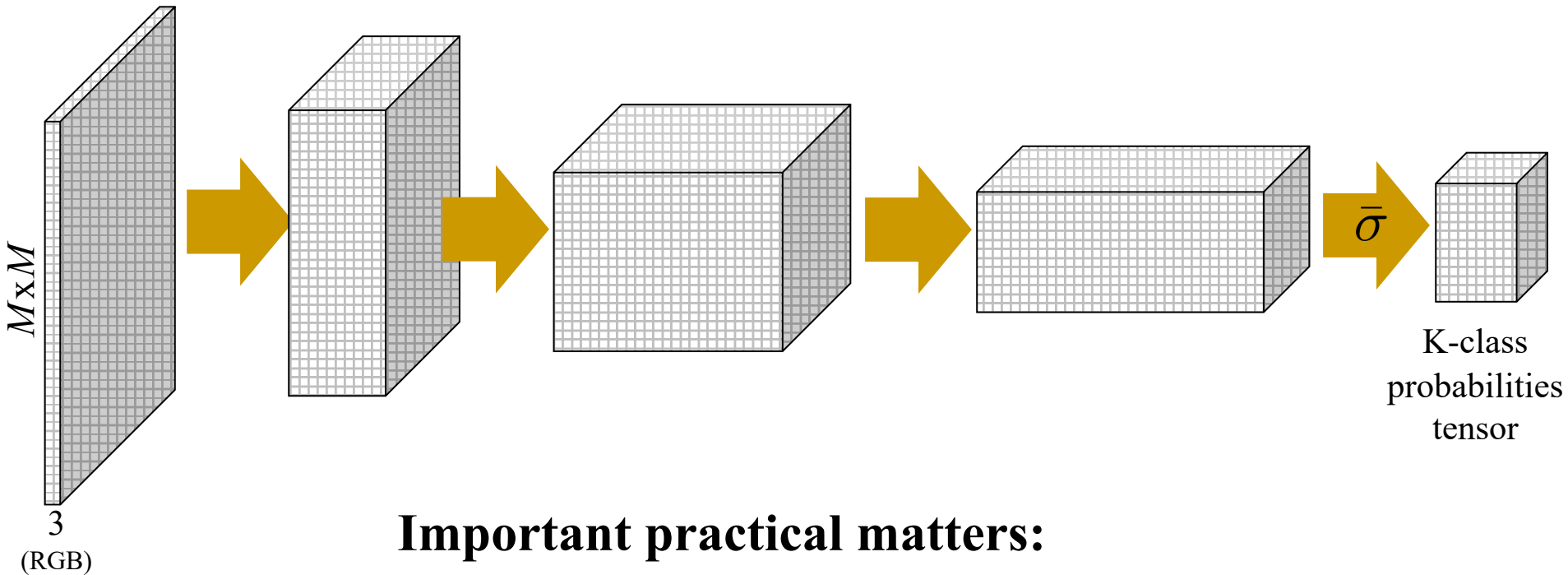
Fully Convolutional Network (FCN)



NOTE: since this network's prediction/output has spatial resolution, it can be trained directly using (**whole**) segmentation masks/targets (unlike our earlier naïve one-pixel classifying network)

Our first “proper” segmentation CNN
end-to-end trainable for image segmentation task

Fully Convolutional Network (FCN)

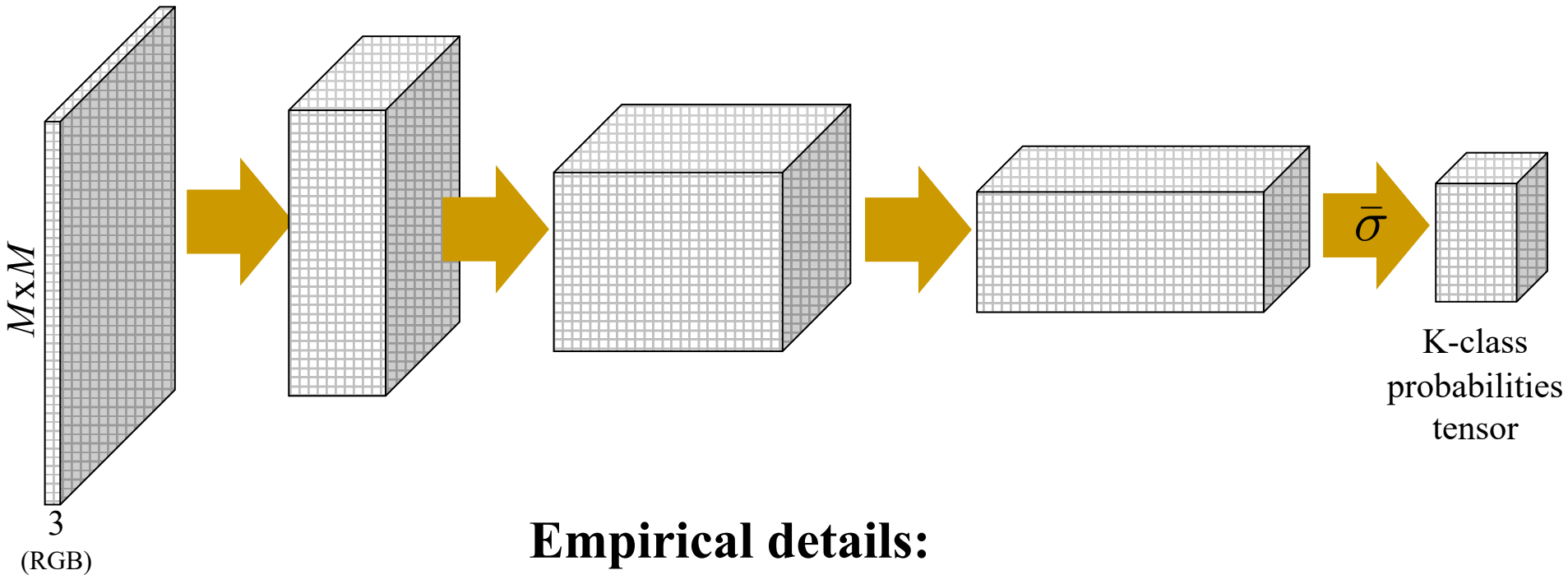


Important practical matters:

FCN can be initialized from network (kernels) **pre-trained on huge image classification training datasets** (e.g. *ResNet* trained on *image net*) learning good high-dimensional features (embedding) at later layers

Then can be **re-trained** (*domain adaptation*) to any specific segmentation dataset **based on full segmentation masks** (targets)

Fully Convolutional Network (FCN)



Empirical details:

works better (after re-training) with **pooling, stride, dilation** giving wider “*receptive field*” for output layer elements/pixels

... even though such operations generally decrease output resolution therefore, requiring **output up-sampling** to improve it

Popular CNN architectures for segmentation

various ideas/details on
pooling, stride, dilation
and upsampling

- **FCN** (2015)

fully convolutional network for segmentation

skip connections

Fully Convolutional Networks for Semantic Segmentation

Long, Shelhamer, Darrell - CVPR 2015

- **SegNet** (2015)

encoder / decoder

Segnet: A deep convolutional encoder-decoder architecture for image segmentation

Badrinarayanan, Kendall, Cipolla – TPAMI 2017

- **UNet** (2015)

encoder / decoder with symmetric skip connections

U-net: Convolutional networks for biomedical image segmentation

Ronneberger, Fischer, Brox - MICCAI 2015 / *Nature Methods* 2019

- **DeepLab** (2015)

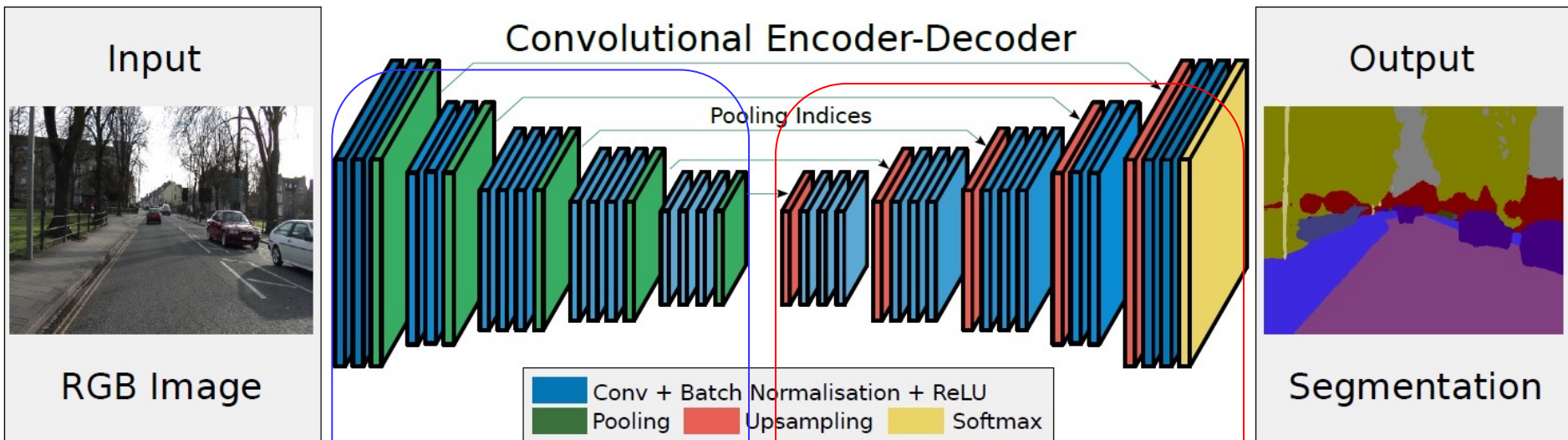
atrous convolutions, spatial pyramid pooling, etc.

DeepLab: Semantic Image Segmentation with Deep Convolutional Nets, Atrous Convolutions, and Fully Connected CRFs

Chen, Papandreou, Kokkinos, Murphy, Yuille – TPAMI 2018 / ICLR 2015

Common Structure: *Encoder/Decoder*

Segnet: A deep convolutional encoder-decoder architecture for image segmentation
Badrinarayanan, Kendall, Cipolla – TPAMI 2017



important:

encoder convolutional layers are typically pre-trained on *image net*

decoder
(upsampling part)

decoder upsamples encoder-generated features

Need for upsampling

Ground truth target



Predicted segmentation

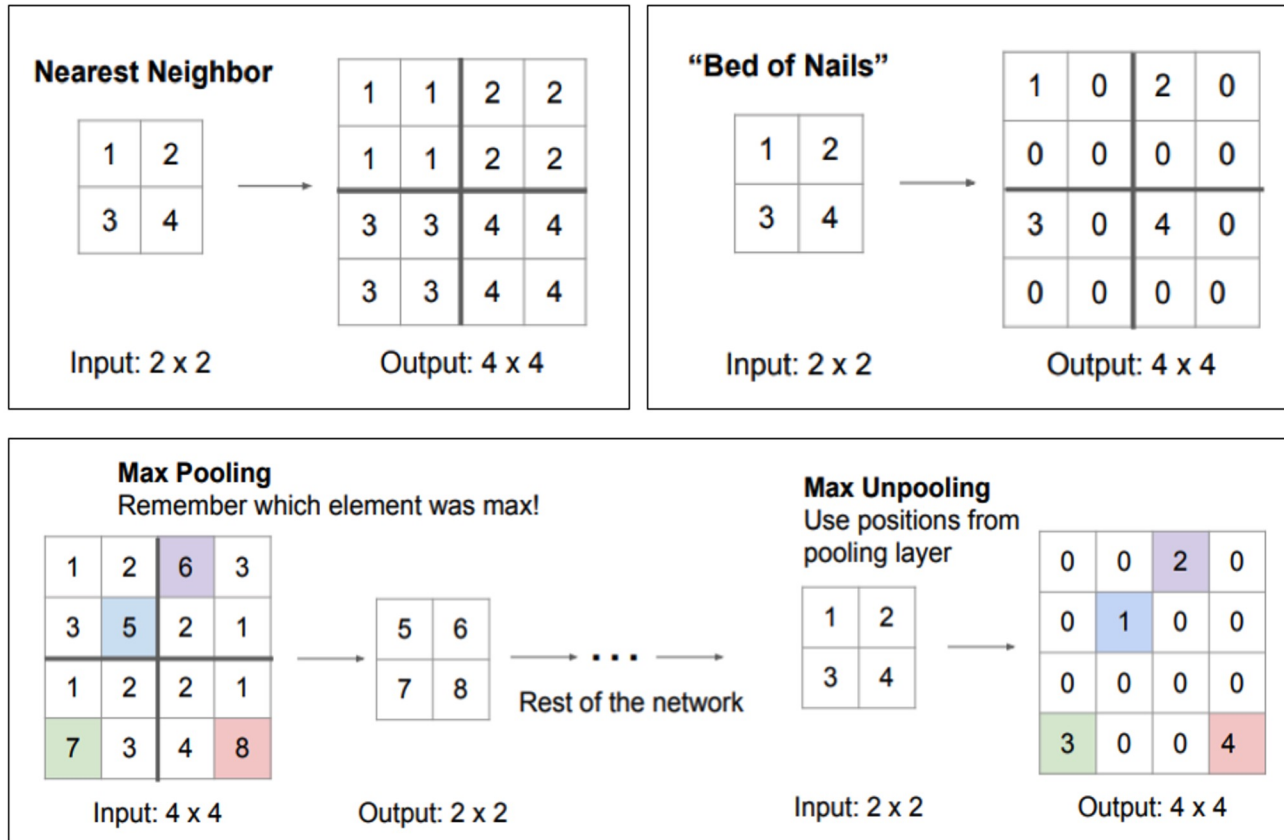


soft-max applied directly to
encoder's output features

Primary goal of the **decoder** is (to learn) **to upsample**

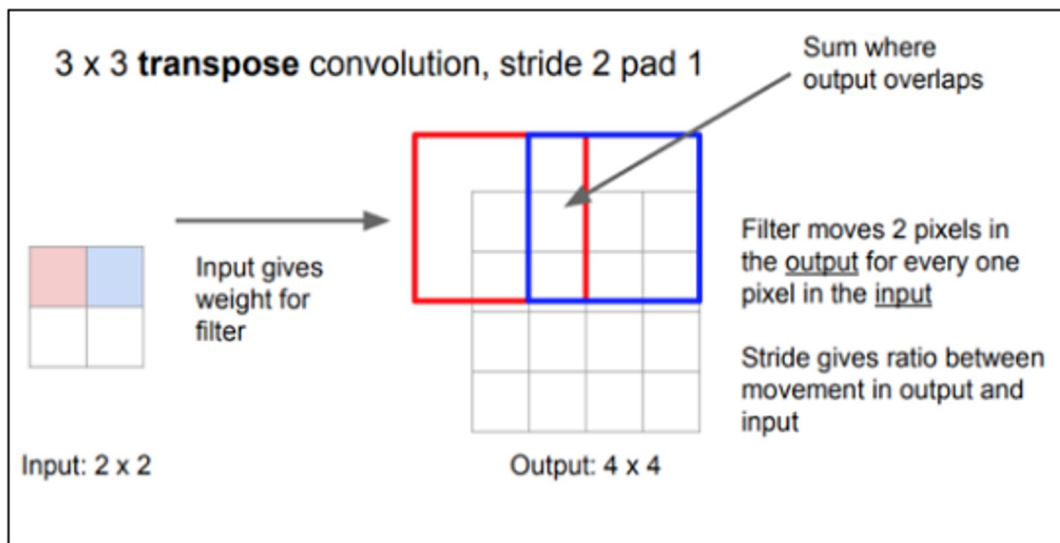
Methods for Upsampling

illustrations credit: Fei-Fei Li

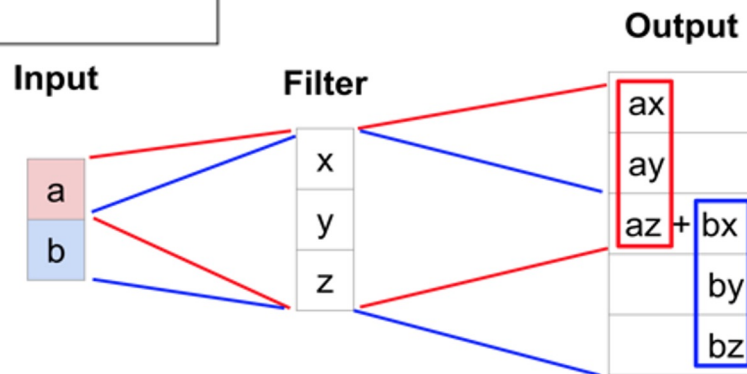


Methods for Upsampling

illustrations credit: Fei-Fei Li



Simpler 1D illustration:



Weights for such **transpose convolution** kernel (filter) **can be learned**.

Why should transpose convolution work well for upsampling?

Transpose Convolution: Example

0	1	2	3
4	5	6	7
8	9	10	11
12	13	14	15

Input Image

Kernel		
0.25	0.5	0.25
0.5	1	0.5
0.25	0.5	0.25

kernel=3x3
stride=2
padding=1

Output Image

Transpose Convolution: Example

First Element x Kernel

0	1	2	3
4	5	6	7
8	9	10	11
12	13	14	15

Input Image

Kernel		
0.25	0.5	0.25
0.5	1	0.5
0.25	0.5	0.25

Element x Kernel

0	0	0
0	0	0
0	0	0

kernel=3x3
stride=2
padding=1

Output Image

Transpose Convolution: Example

Added Result

0	1	2	3
4	5	6	7
8	9	10	11
12	13	14	15

Input Image

Kernel		
0.25	0.5	0.25
0.5	1	0.5
0.25	0.5	0.25

Element x Kernel

0	0	0
0	0	0
0	0	0

kernel=3x3
stride=2
padding=1

Output Image

0	0	0						
0	0	0						
0	0	0						

Transpose Convolution: Example

Next Element x Kernel

0	1	2	3
4	5	6	7
8	9	10	11
12	13	14	15

Input Image

Kernel

0.25	0.5	0.25
0.5	1	0.5
0.25	0.5	0.25

Element x Kernel

0.25	0.5	0.25
0.5	1	0.5
0.25	0.5	0.25

kernel=3x3
stride=2
padding=1

Output Image

0	0	0						
0	0	0						
0	0	0						

Transpose Convolution: Example

Added Result

0	1	2	3
4	5	6	7
8	9	10	11
12	13	14	15

Input Image

Kernel		
0.25	0.5	0.25
0.5	1	0.5
0.25	0.5	0.25

Element x Kernel

0.25	0.5	0.25
0.5	1	0.5
0.25	0.5	0.25

kernel=3x3
stride=2
padding=1

Output Image

0	0	0.25	0.5	0.25				
0	0	0.5	1	0.5				
0	0	0.25	0.5	0.25				

Transpose Convolution: Example

Next Element x Kernel

0	1	2	3
4	5	6	7
8	9	10	11
12	13	14	15

Input Image

Kernel

0.25	0.5	0.25
0.5	1	0.5
0.25	0.5	0.25

Element x Kernel

0.5	1	0.5
1	2	1
0.5	1	0.5

kernel=3x3
stride=2
padding=1

Output Image

0	0	0.25	0.5	0.25				
0	0	0.5	1	0.5				
0	0	0.25	0.5	0.25				

Transpose Convolution: Example

Added Result

0	1	2	3
4	5	6	7
8	9	10	11
12	13	14	15

Input Image

Kernel

0.25	0.5	0.25
0.5	1	0.5
0.25	0.5	0.25

Element x Kernel

0.5	1	0.5
1	2	1
0.5	1	0.5

kernel=3x3
stride=2
padding=1

Output Image

0	0	0.25	0.5	0.75	1	0.5		
0	0	0.5	1	1.5	2	1		
0	0	0.25	0.5	0.75	1	0.5		

Transpose Convolution: Example

Next Element x Kernel

0	1	2	3
4	5	6	7
8	9	10	11
12	13	14	15

Input Image

Kernel

0.25	0.5	0.25
0.5	1	0.5
0.25	0.5	0.25

Element x Kernel

0.75	1.5	0.75
1.5	3	1.5
0.75	1.5	0.75

kernel=3x3
stride=2
padding=1

Output Image

0	0	0.25	0.5	0.75	1	0.5		
0	0	0.5	1	1.5	2	1		
0	0	0.25	0.5	0.75	1	0.5		

Transpose Convolution: Example

Added Result

0	1	2	3
4	5	6	7
8	9	10	11
12	13	14	15

Input Image

Kernel

0.25	0.5	0.25
0.5	1	0.5
0.25	0.5	0.25

Element x Kernel

0.75	1.5	0.75
1.5	3	1.5
0.75	1.5	0.75

kernel=3x3
stride=2
padding=1

Output Image

0	0	0.25	0.5	0.75	1	1.25	1.5	0.75
0	0	0.5	1	1.5	2	2.5	3	1.5
0	0	0.25	0.5	0.75	1	1.25	1.5	0.75

Transpose Convolution: Example

Next Element x Kernel

0	1	2	3
4	5	6	7
8	9	10	11
12	13	14	15

Input Image

Kernel

0.25	0.5	0.25
0.5	1	0.5
0.25	0.5	0.25

Element x Kernel

1	2	1
2	4	2
1	2	1

kernel=3x3
stride=2
padding=1

Output Image

0	0	0.25	0.5	0.75	1	1.25	1.5	0.75
0	0	0.5	1	1.5	2	2.5	3	1.5
0	0	0.25	0.5	0.75	1	1.25	1.5	0.75

Transpose Convolution: Example

Added Result

0	1	2	3
4	5	6	7
8	9	10	11
12	13	14	15

Input Image

Kernel

0.25	0.5	0.25
0.5	1	0.5
0.25	0.5	0.25

Element x Kernel

1	2	1
2	4	2
1	2	1

kernel=3x3
stride=2
padding=1

Output Image

0	0	0.25	0.5	0.75	1	1.25	1.5	0.75
0	0	0.5	1	1.5	2	2.5	3	1.5
1	2	1.25	0.5	0.75	1	1.25	1.5	0.75
2	4	2						
1	2	1						

Transpose Convolution: Example

Added Result

0	1	2	3
4	5	6	7
8	9	10	11
12	13	14	15

Input Image

Kernel

0.25	0.5	0.25
0.5	1	0.5
0.25	0.5	0.25

Element x Kernel

1.25	2.5	1.25
2.5	5	2.5
1.25	2.5	1.5

kernel=3x3
stride=2
padding=1

Output Image

0	0	0.25	0.5	0.75	1	1.25	1.5	0.75
0	0	0.5	1	1.5	2	2.5	3	1.5
1	2	2.5	3	2	1	1.25	1.5	0.75
2	4	4.5	5	2.5				
1	2	2.5	2.5	1.5				

Transpose Convolution: Example

Added Result

0	1	2	3
4	5	6	7
8	9	10	11
12	13	14	15

Input Image

Kernel

0.25	0.5	0.25
0.5	1	0.5
0.25	0.5	0.25

Element x Kernel

1.5	3	1.5
3	6	3
1.5	3	1.5

kernel=3x3
stride=2
padding=1

Output Image

0	0	0.25	0.5	0.75	1	1.25	1.5	0.75
0	0	0.5	1	1.5	2	2.5	3	1.5
1	2	2.5	3	3.5	4	2.75	1.5	0.75
2	4	4.5	5	5.5	6	3		
1	2	2.5	2.5	2.75	3	1.5		

Transpose Convolution: Example

Added Result

0	1	2	3
4	5	6	7
8	9	10	11
12	13	14	15

Input Image

Kernel

0.25	0.5	0.25
0.5	1	0.5
0.25	0.5	0.25

Element x Kernel

1.75	3.5	1.75
3.5	7	3.5
1.75	3.5	1.75

kernel=3x3
stride=2
padding=1

Output Image

0	0	0.25	0.5	0.75	1	1.25	1.5	0.75
0	0	0.5	1	1.5	2	2.5	3	1.5
1	2	2.5	3	3.5	4	4.5	5	2.5
2	4	4.5	5	5.5	6	6.5	7	3.5
1	2	2.5	2.5	2.75	3	3.25	3.5	1.75

Transpose Convolution: Example

Added Result

0	1	2	3
4	5	6	7
8	9	10	11
12	13	14	15

Input Image

Kernel		
0.25	0.5	0.25
0.5	1	0.5
0.25	0.5	0.25

Element x Kernel

2	4	2
4	8	4
2	4	2

kernel=3x3
stride=2
padding=1

Output Image

0	0	0.25	0.5	0.75	1	1.25	1.5	0.75
0	0	0.5	1	1.5	2	2.5	3	1.5
1	2	2.5	3	3.5	4	4.5	5	2.5
2	4	4.5	5	5.5	6	6.5	7	3.5
3	6	4.25	2.5	2.75	3	3.25	3.5	1.75
4	8	4						
2	4	2						

Transpose Convolution: Example

Added Result

0	1	2	3
4	5	6	7
8	9	10	11
12	13	14	15

Input Image

Kernel		
0.25	0.5	0.25
0.5	1	0.5
0.25	0.5	0.25

Element x Kernel

3.75	7.5	3.75
7.5	15	7.5
3.75	7.5	3.75

kernel=3x3
stride=2
padding=1

Output Image

0	0	0.25	0.5	0.75	1	1.25	1.5	0.75
0	0	0.5	1	1.5	2	2.5	3	1.5
1	2	2.5	3	3.5	4	4.5	5	2.5
2	4	4.5	5	5.5	6	6.5	7	3.5
3	6	6.5	7	7.5	8	8.5	9	4.5
4	8	8.5	9	9.5	10	10.5	11	5.5
5	10	10.5	11	11.5	12	12.5	13	6.5
6	12	12.5	13	13.5	14	14.5	15	7.5
3	6	6.25	6.5	6.75	7	7.25	7.5	3.75

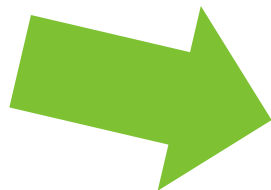
Transpose Convolution: Example

Note: this result is equivalent to **Bilinear Interpolation**

0	1	2	3
4	5	6	7
8	9	10	11
12	13	14	15

Input Image

Kernel		
0.25	0.5	0.25
0.5	1	0.5
0.25	0.5	0.25



kernel=3x3
stride=2
padding=1

Output Image

0	0	0.25	0.5	0.75	1	1.25	1.5	0.75
0	0	0.5	1	1.5	2	2.5	3	1.5
4	2	2.5	3	3.5	4	4.5	5	2.5
2	4	4.5	5	5.5	6	6.5	7	3.5
3	6	6.5	7	7.5	8	8.5	9	4.5
4	8	8.5	9	9.5	10	10.5	11	5.5
5	10	10.5	11	11.5	12	12.5	13	6.5
6	12	12.5	13	13.5	14	14.5	15	7.5
3	6	6.25	6.5	6.75	7	7.25	7.5	3.75

Bilinear Interpolation is a special case of transpose convolution.

The corresponding transpose convolution kernels exists for any stride (code <https://gist.github.com/mjstevens777/9d6771c45f444843f9e3dce6a401b183>)

V. Dumoulin, and F. Visin. "A guide to convolution arithmetic for deep learning." *arXiv preprint arXiv:1603.07285* (2016).

Transpose Convolution and Bilinear Interpolation

Thus...

the transpose convolution should be at least as good as bilinear interpolation.

In particular, transpose convolution kernel can be initialized to replicate bilinear interpolation, but one might learn a “better” upsampling kernel during training.

Transpose Convolution: other names

- ***Deconvolution***: not a very good name as it is commonly used for the inverse of convolution. Moreover, in image analysis, “*deconvolution*” also stands for a standard non-linear image reconstruction problem.
- ***Backward convolution***: If we think about convolution of an input image as a matrix multiplication operation, then transposed convolution could be related to the backward pass when the loss gradient is backpropagated through the standard convolutional layer.
- ***Fractionally-strided convolution***: transposed convolution with stride s is equivalent to a standard convolution with stride $1/s$, as follows: insert $(s-1)$ zeros between pixels, then apply regular conv using the same kernel (see **example on the next slide**).

Fractionally-strided Convolution

Fractional Stride

0	1	2	3
4	5	6	7
8	9	10	11
12	13	14	15

Input Image

Kernel		
0.25	0.5	0.25
0.5	1	0.5
0.25	0.5	0.25

Standard Convolution

kernel=3x3
stride= $\frac{1}{2}$
(inserting one zero
between pixels, then
apply conv with stride=1)
padding=1



Transposed Convolution

kernel=3x3
stride=2
padding=1

Zero-interleaved Image (also zero-padded)

0	0	0	0	0	0	0	0	0
0	0	0	1	0	2	0	3	0
0	0	0	0	0	0	0	0	0
0	4	0	5	0	6	0	7	0
0	0	0	0	0	0	0	0	0
0	8	0	9	0	10	0	11	0
0	0	0	0	0	0	0	0	0
0	12	0	13	0	14	0	15	0
0	0	0	0	0	0	0	0	0

Now, apply standard convolution...

Fractionally-strided Convolution

Zero-interleaved Image
(also zero-padded)

0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0

standard
convolution



with
kernel

0.25	0.5	0.25
0.5	1	0.5
0.25	0.5	0.25

0	0.5	1	1.5	2	2.5	3
2	2.5	3	3.5	4	4.5	5
4	4.5	5	5.5	6	6.5	7
6	6.5	7	7.5	8	8.5	9
8	8.5	9	9.5	10	10.5	11
10	10.5	11	11.5	12	12.5	13
12	12.5	13	13.5	14	14.5	15

Output

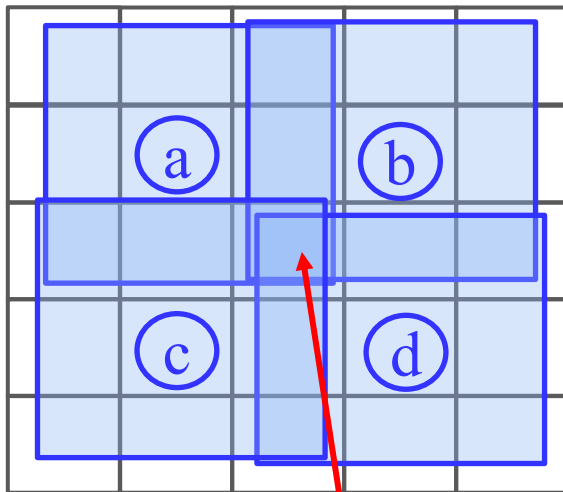
Transposed vs Fractionally-strided Convolution

Upsampling Example:

a	b
c	d



transpose convolution (slide 26)



kernel k

$k_{-1,-1}$	$k_{0,-1}$	$k_{1,-1}$
$k_{-1,0}$	$k_{0,0}$	$k_{1,0}$
$k_{-1,1}$	$k_{0,1}$	$k_{1,1}$

output of transpose convolution using k
with stride 2 for the **pixel in the center**

$$ak_{1,1} + bk_{-1,1} + ck_{1,-1} + dk_{-1,-1}$$

fractionally-strided convolution

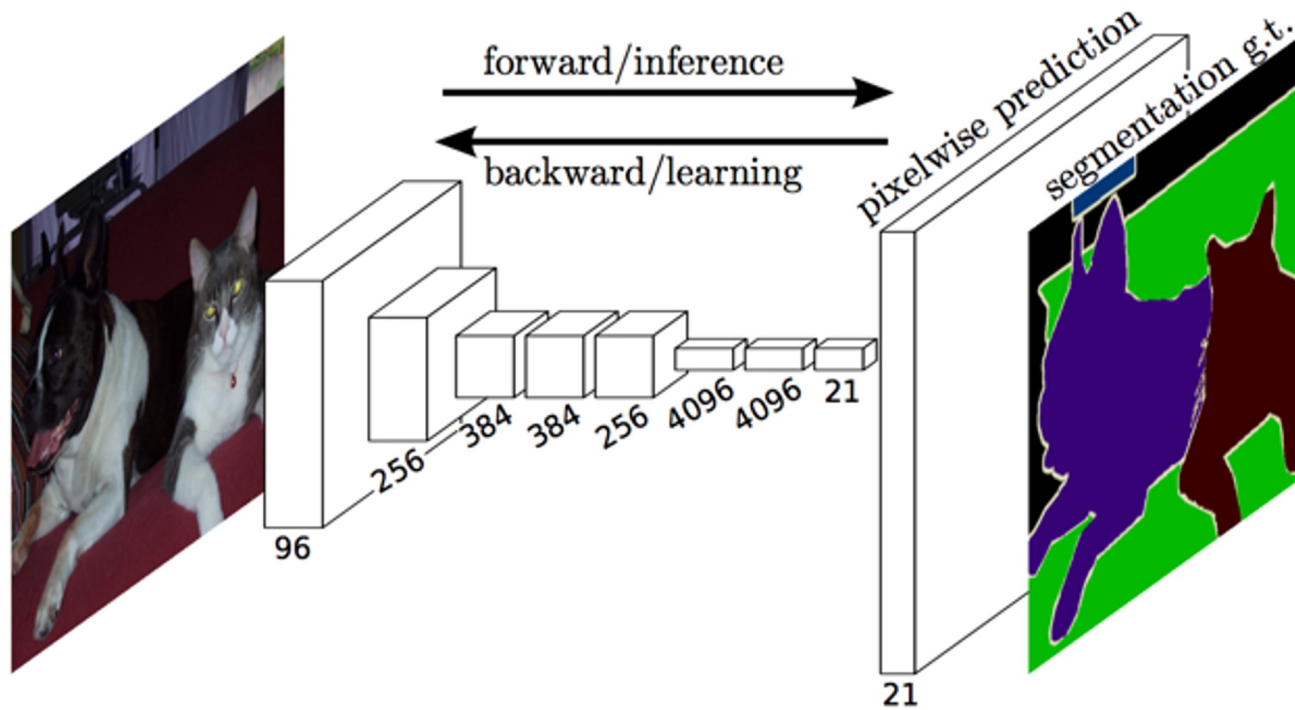
0	0	0	0	0
0	a	0	b	0
0	0	0	0	0
0	c	0	d	0
0	0	0	0	0

output of standard convolution using k
with stride 1/2 for the **pixel in the center**

$$ak_{-1,-1} + bk_{1,-1} + ck_{-1,1} + dk_{1,1}$$

For non-symmetric kernels one must use a “transposed” version of the kernel (flipped both horizontally & vertically) to get equivalence between the transposed convolution (as on slide 26) and the fractionally-strided convolution.

Fully Convolutional Networks (FCNs)

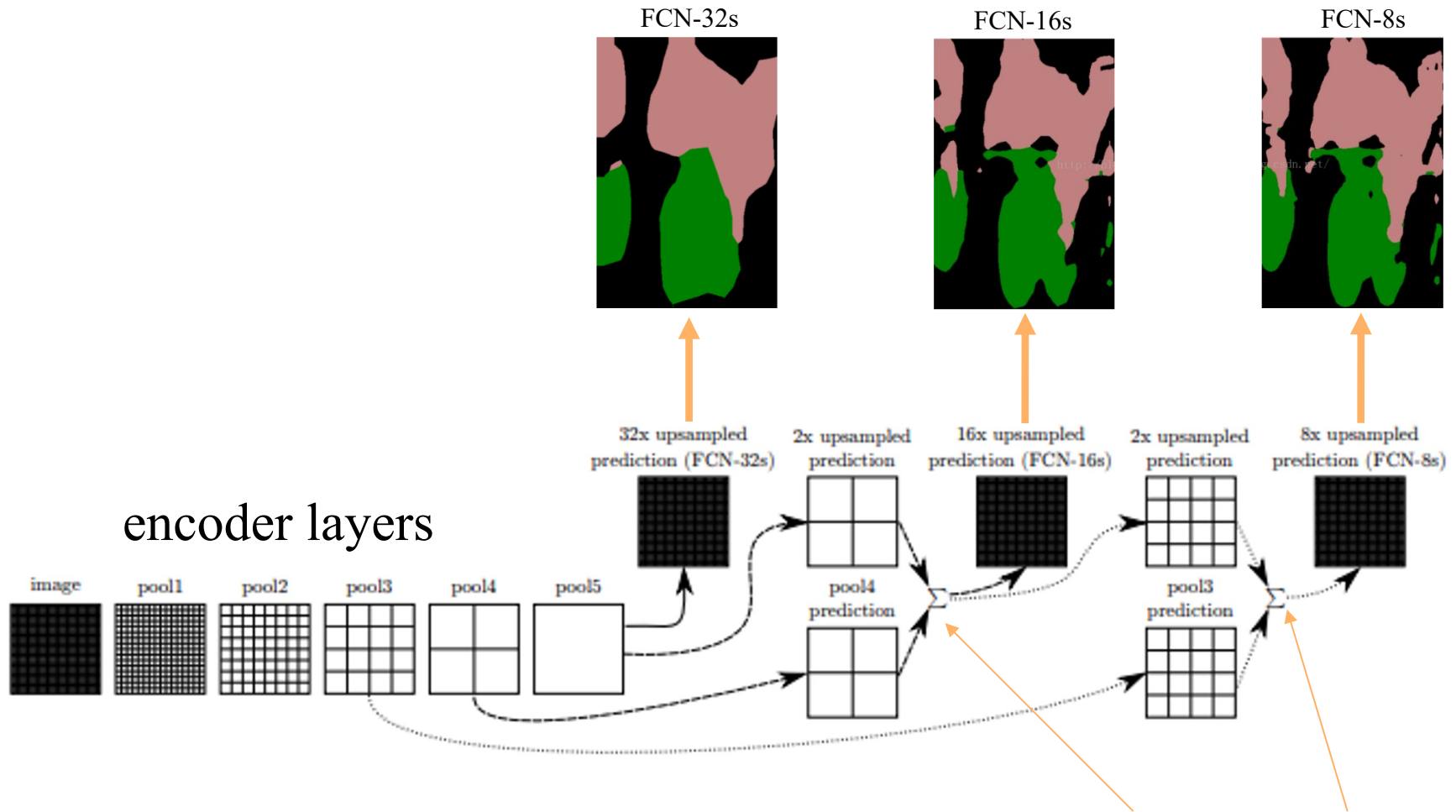


Upsample segmentation using “**deconvoluton**” *transposed convolution*

Fully Convolutional Networks for Semantic Segmentation

Long, Shelhamer, Darrell - CVPR 2015

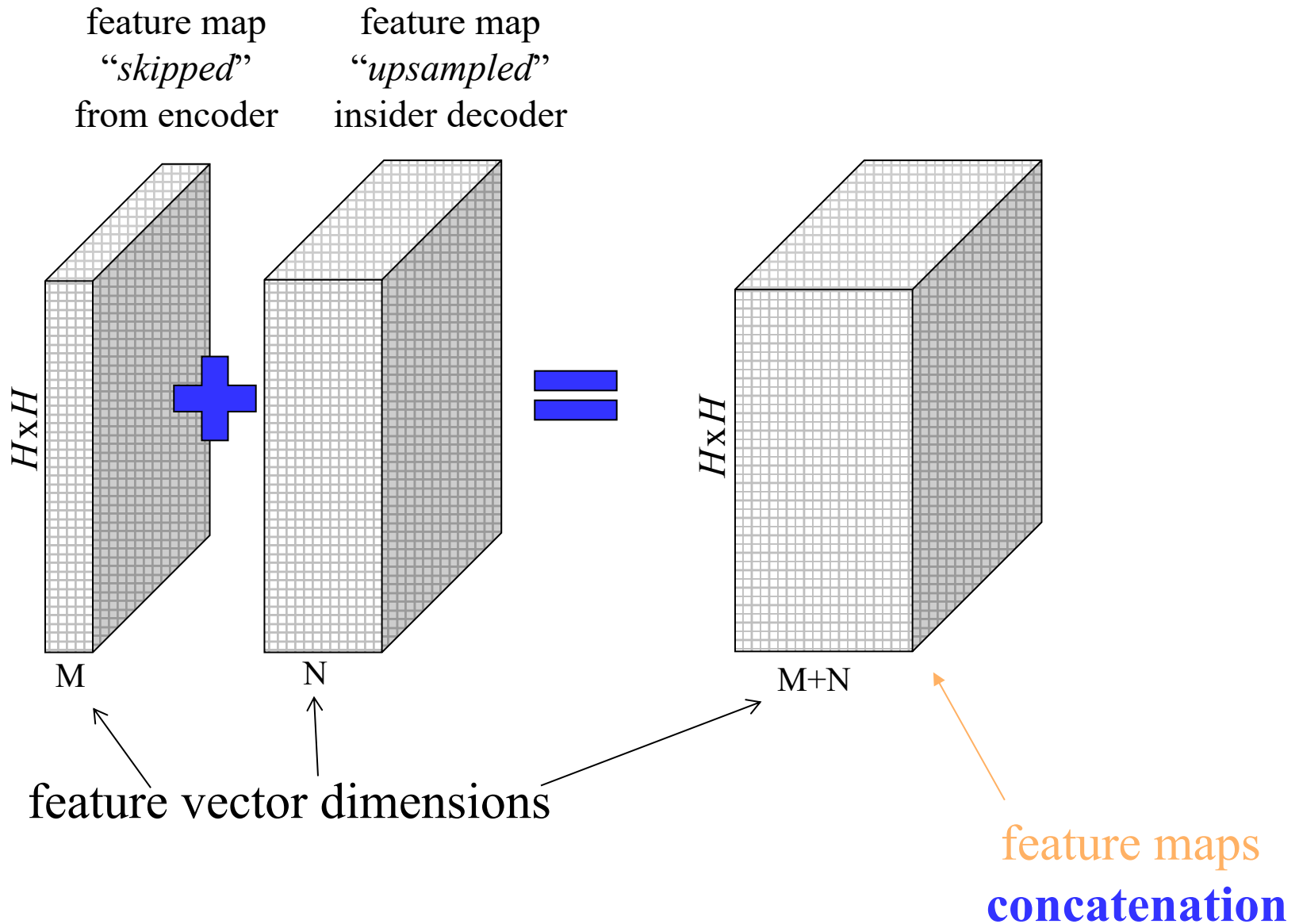
Upsampling using skip connections



Fully Convolutional Networks for Semantic Segmentation
Long, Shelhamer, Darrell - CVPR 2015

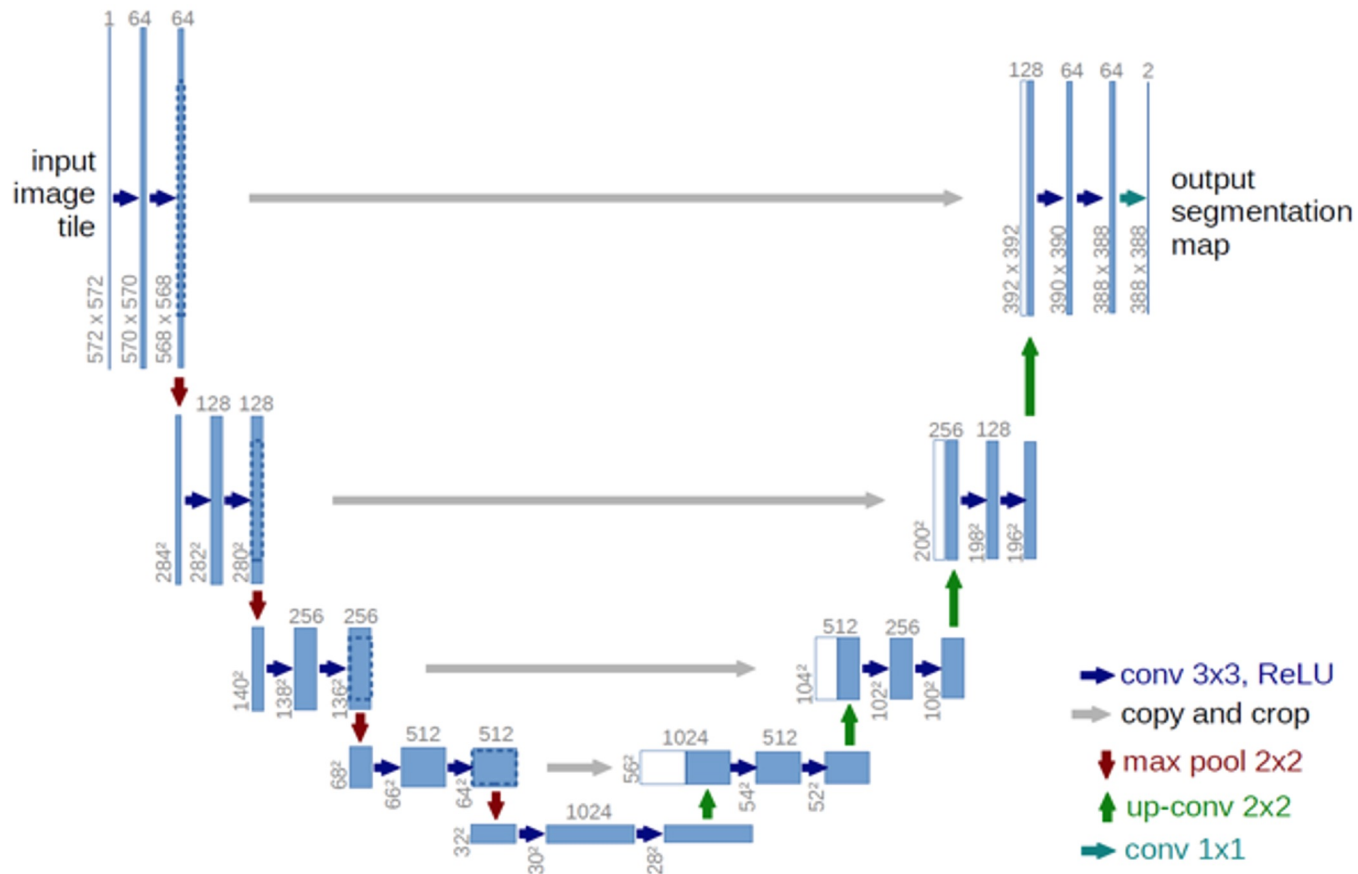
feature maps
concatenation

Skip connections: concatenation



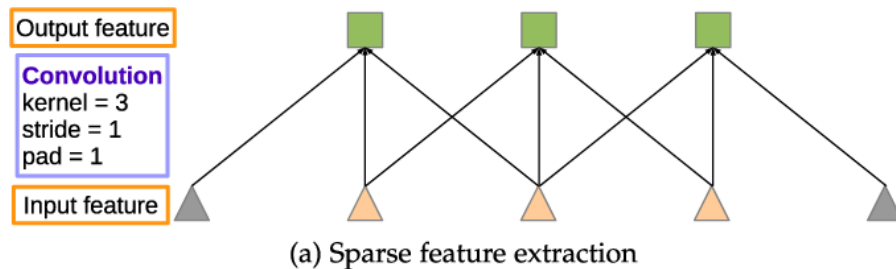
U-net: expanding decoder with symmetry

and many **skip connections**

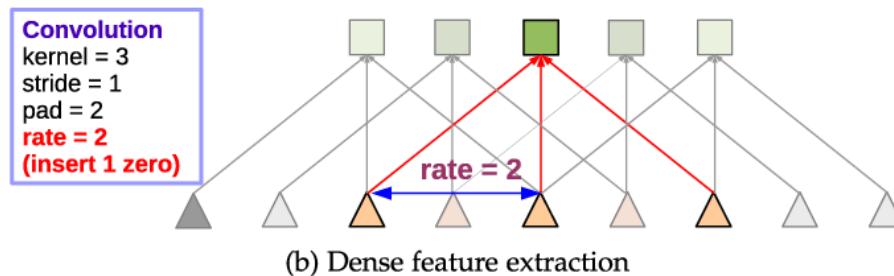


DeepLab

- encoder uses ***atrous convolutions*** (a.k.a. *dilation*)
increasing *receptive field* without increase in kernel size
(or significant decrease in output resolution)



standard 3x3 convolution



atrous 3x3 convolution
i.e. convolution with
holes or gaps (Fr. *trous*)

Key insight: encoder can still use any standard kernels
pre-trained on *image-net* classification (e.g. from *ResNet*)
For example, pre-trained 3x3 kernels can be “dilated” into
5x5 kernels (as above) by adding “holes”

DeepLab

- encoder uses *atrous convolutions* (a.k.a. *dilation*)
increasing *receptive field* without significant loss of resolution
(unlike stride and pooling)
- decoder uses *bilinear interpolation* (see topic 4)
for upsampling
- other ideas

(Training) Loss: Cross-Entropy

(GT mask)

image sample i



network prediction



pixel-precise target



$$\bar{\sigma}^p = (\bar{\sigma}_1, \bar{\sigma}_2, \dots, \bar{\sigma}_K)$$

prediction at each pixel p

$$\mathbf{y}^p \in [0, 1, 2, 3, \dots] \quad - \quad \text{class label at each pixel } p$$

$$\bar{\mathbf{y}}^p = (0, 0, 1, 0, \dots, 0) \quad - \quad \text{one-hot distribution at } p$$

**Loss over
image i :**

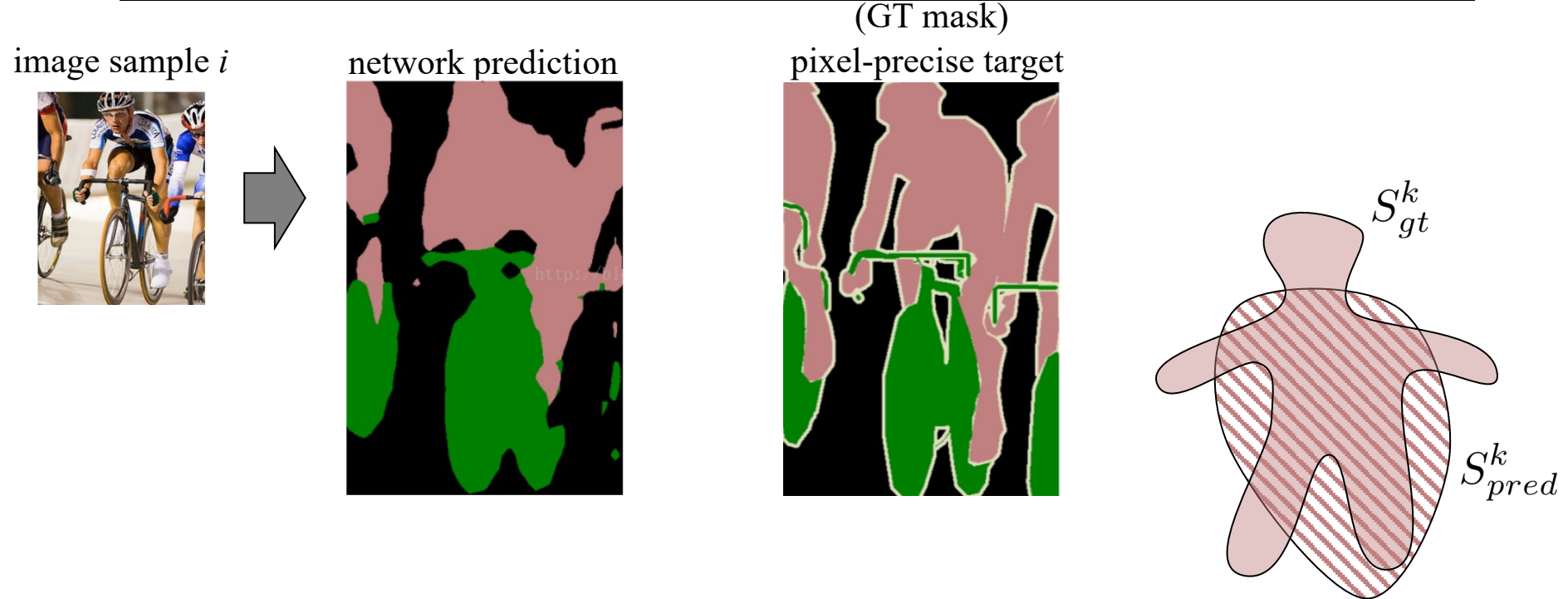
$$\sum_{p \in I_i} \overbrace{\sum_k -\bar{\mathbf{y}}_k^p \ln \bar{\sigma}_k^p}^{\text{cross entropy at } p}$$

sum of
negative log-likelihoods (NLL)

$$= - \sum_{p \in I_i} \ln \bar{\sigma}_{\mathbf{y}^p}^p$$

Total loss should also sum over all images i

(Validation) Quality Metrics



- *Mean intersection over union* $\text{mIoU} = \frac{1}{K} \sum_k \frac{|S_{gt}^k \cap S_{pred}^k|}{|S_{gt}^k \cup S_{pred}^k|} \in [0, 1]$
(focus on segments/classes, object sizes are irrelevant)
- There are also accuracy measures focused on pixels
(what percentage of pixels is correctly classified)